
计算光学成像与光信息技术前沿

第十二周课 (lecture 8)

差分相衬成像

左超

南京理工大学电光学院光电技术系

Jiangsu Key Laboratory of Spectral Imaging & Intelligent Sense (SIIS)

Nanjing University of Science and Technology,

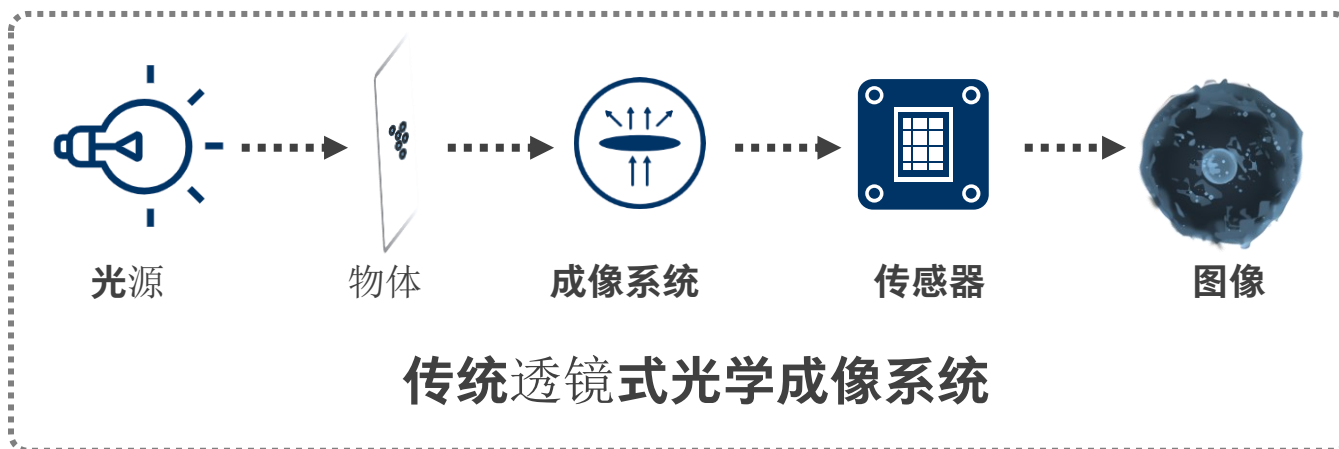
Nanjing, Jiangsu Province 210094, China



电子工程与光电技术学院
School of Electronic and Optical Engineering

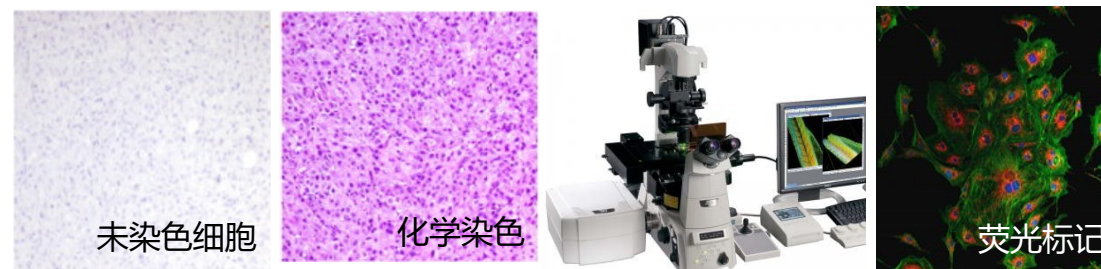


江苏省光谱成像与智能感知重点实验室
Jiangsu Key Laboratory of Spectral Imaging & Intelligent Sense



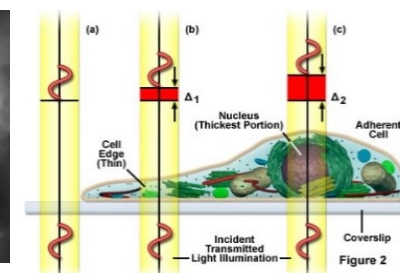
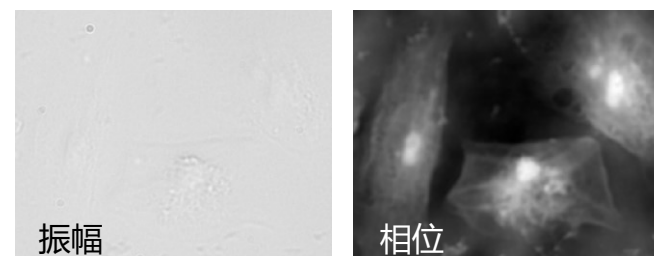
传统透镜式成像
点对点光强信号探测

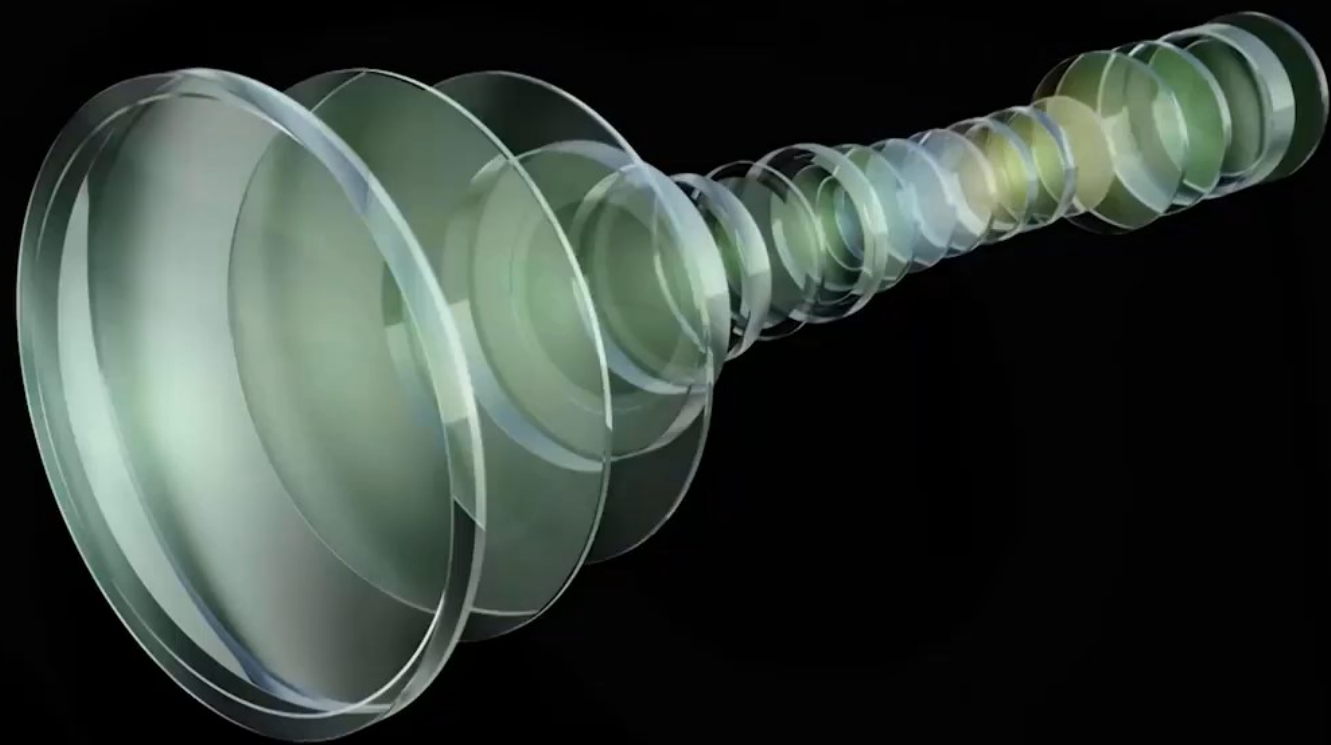
- 成像依赖染色标记
- 无法定量探测相位



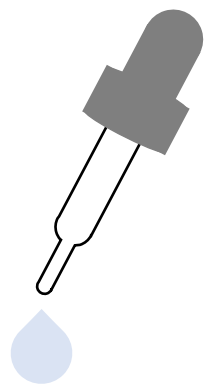
侵入式成像
(Invasive)

无标记成像
(Label-free)





Staining and fluorescence (a)



Fluorescence techniques

Confocal microscopy;
Total internal reflection fluorescence;
Two/multi-photon microscopy;
Light-sheet microscopy;
...

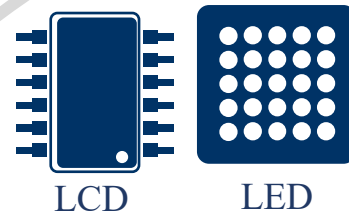
Super-resolution fluorescence techniques

Stimulated emission depletion microscopy;
Photoactivated localization microscopy;
Stochastic optical reconstruction microscopy;
Structured illumination microscopy;
...

Phase contrast techniques

Zernike phase-contrast microscopy
Differential interference contrast microscopy
...

Contrast

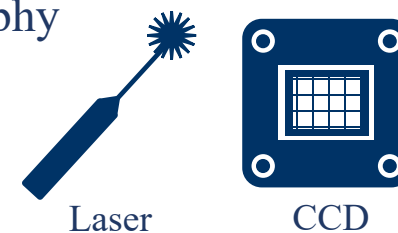


Noninterferometric QPI techniques

Transport-of-intensity equation;
Differential phase contrast;
Fourier ptychographic microscopy;
Lens-free on-chip holography;
...

Optical interferometry and holography

Digital holographic microscopy



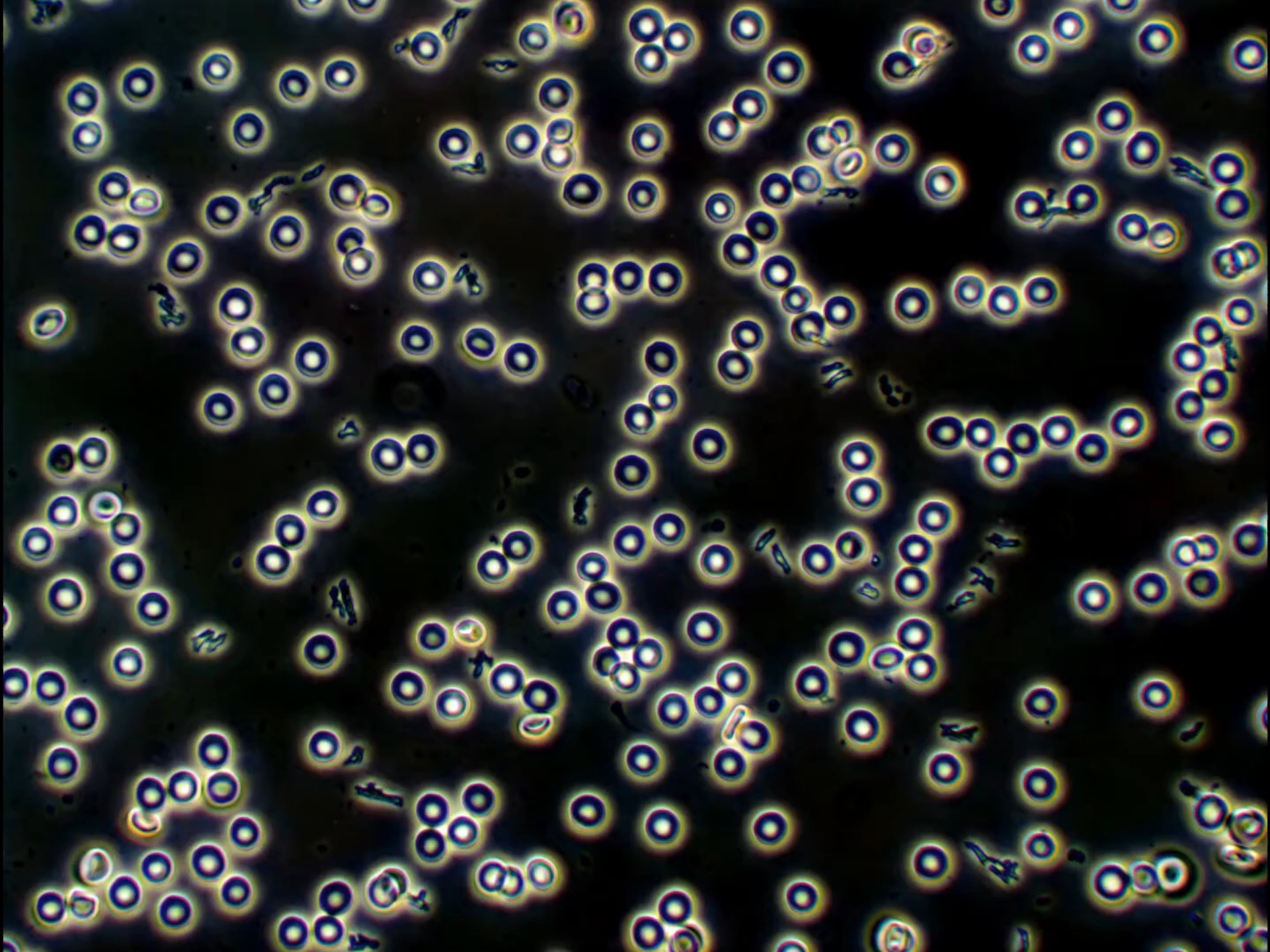
Computational light microscopy

(b) Phase changes

“无标记”相衬成像技术

暗场显微镜





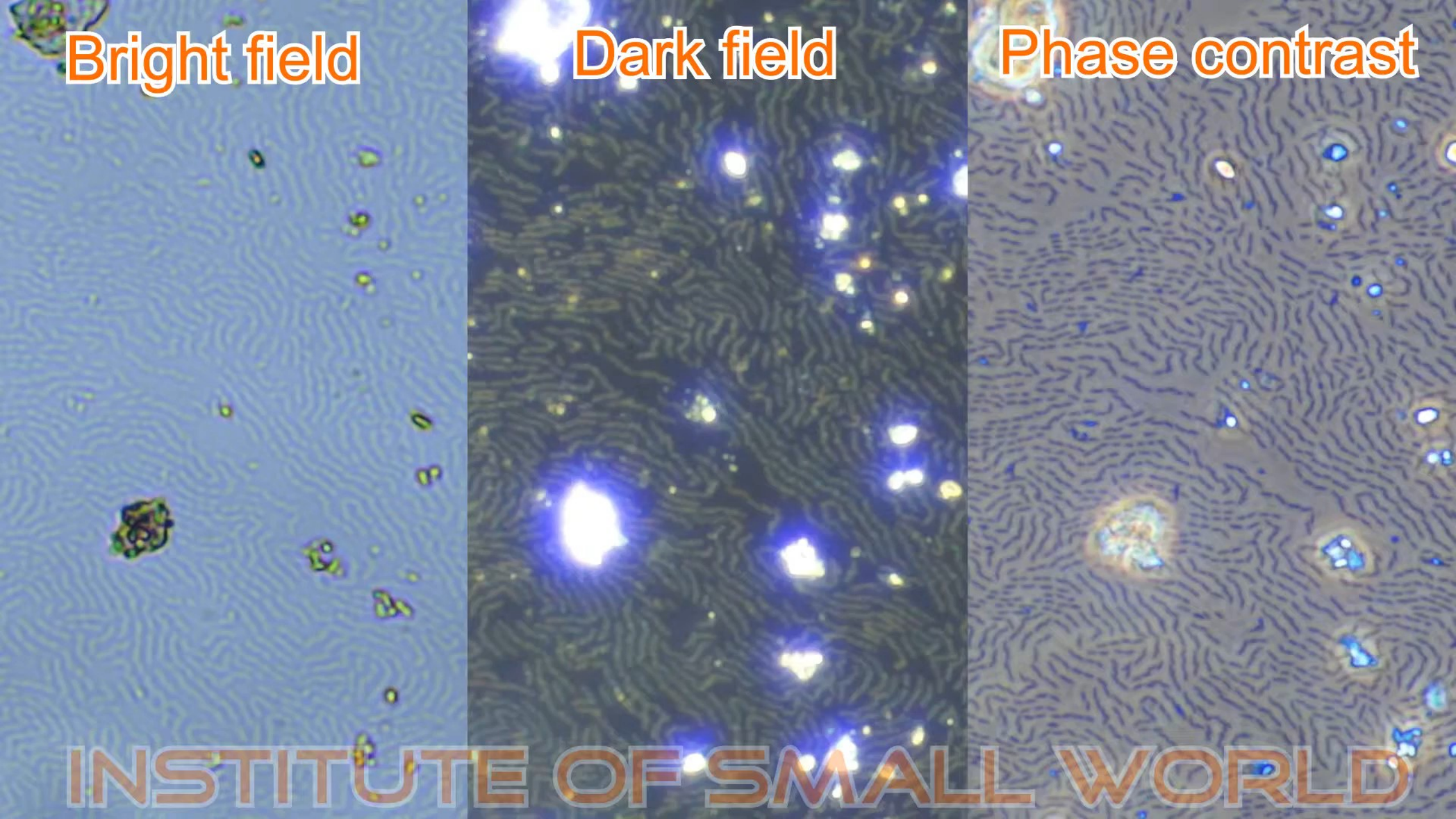
Dark field and phase contrast microscopes

Bright field

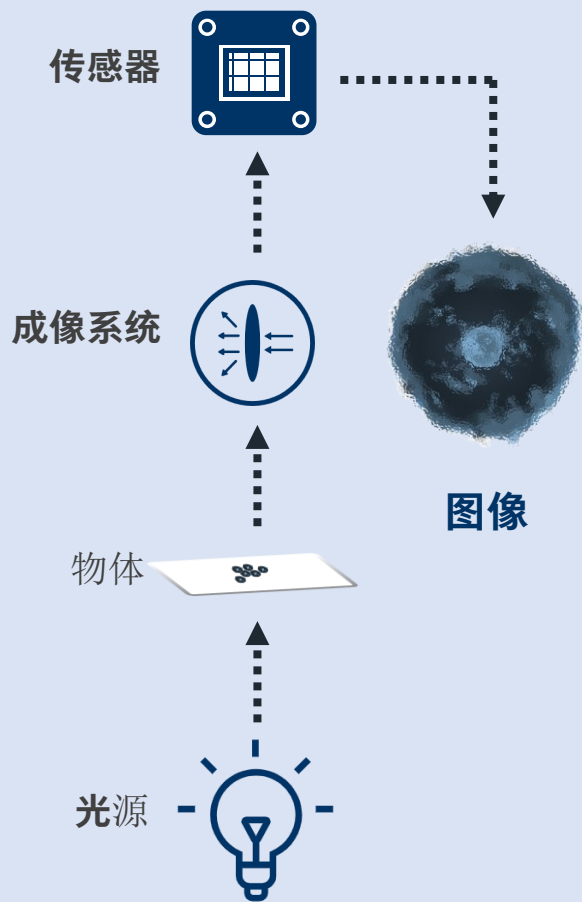
Dark field

Phase contrast

INSTITUTE OF SMALL WORLD

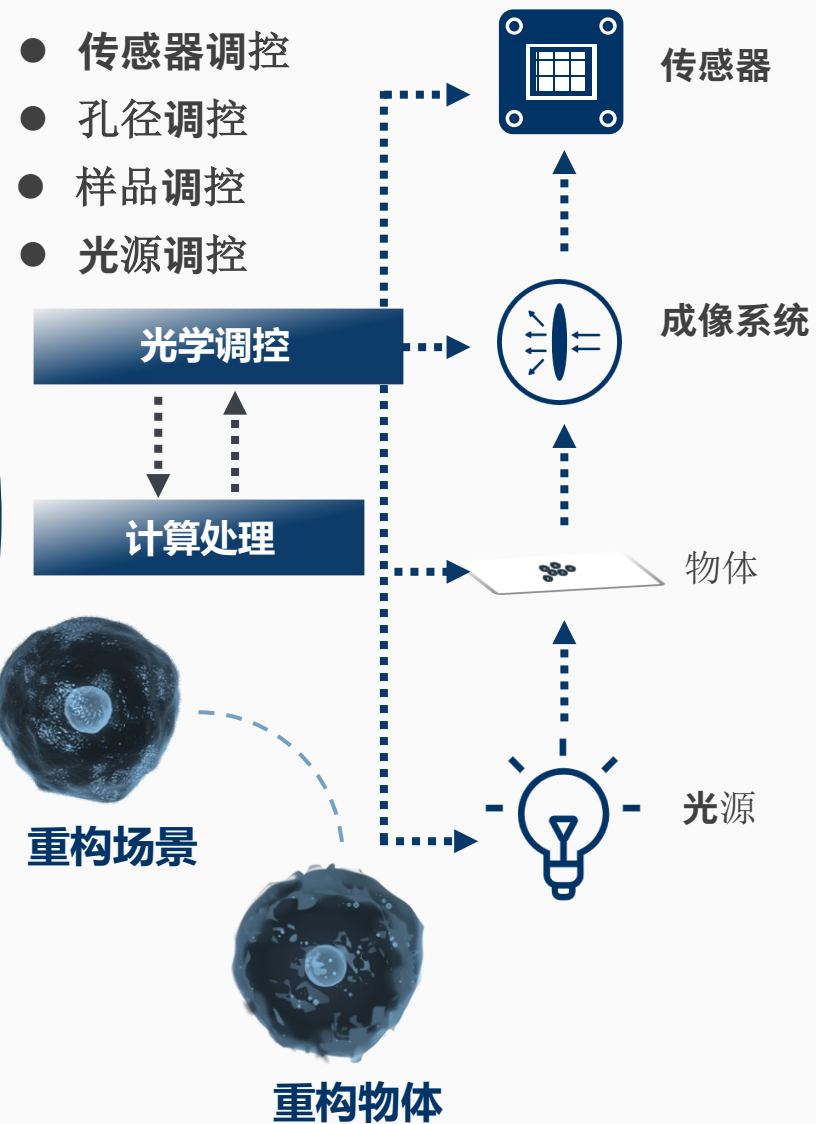





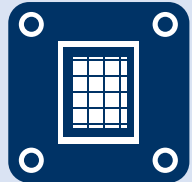
传统显微成像



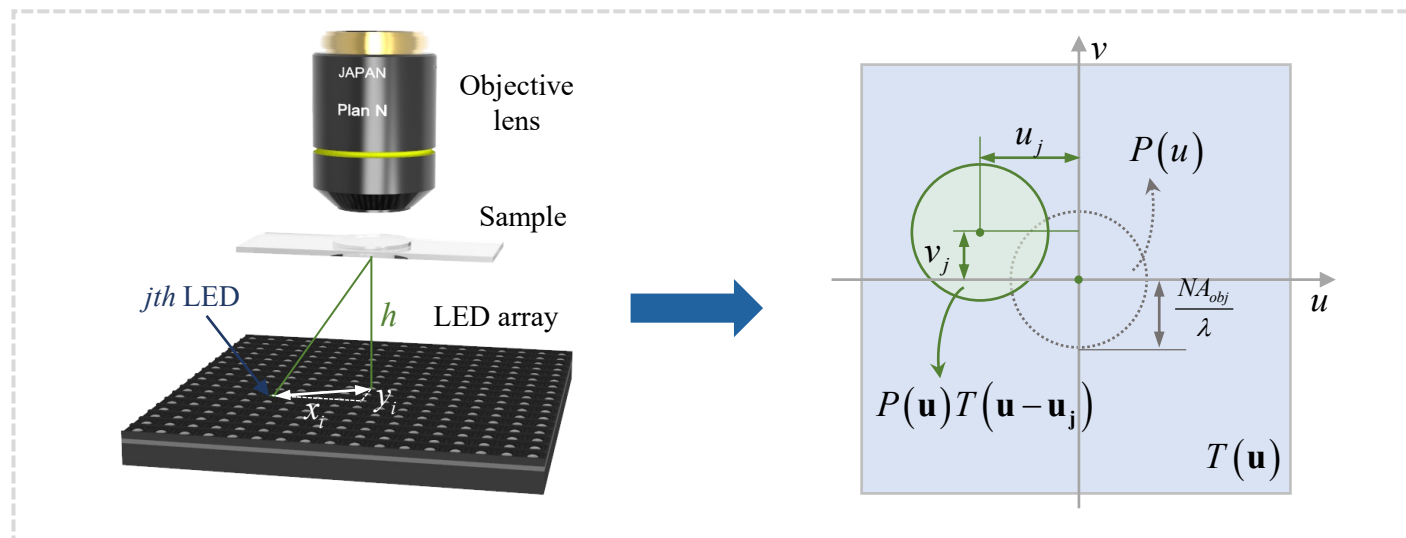
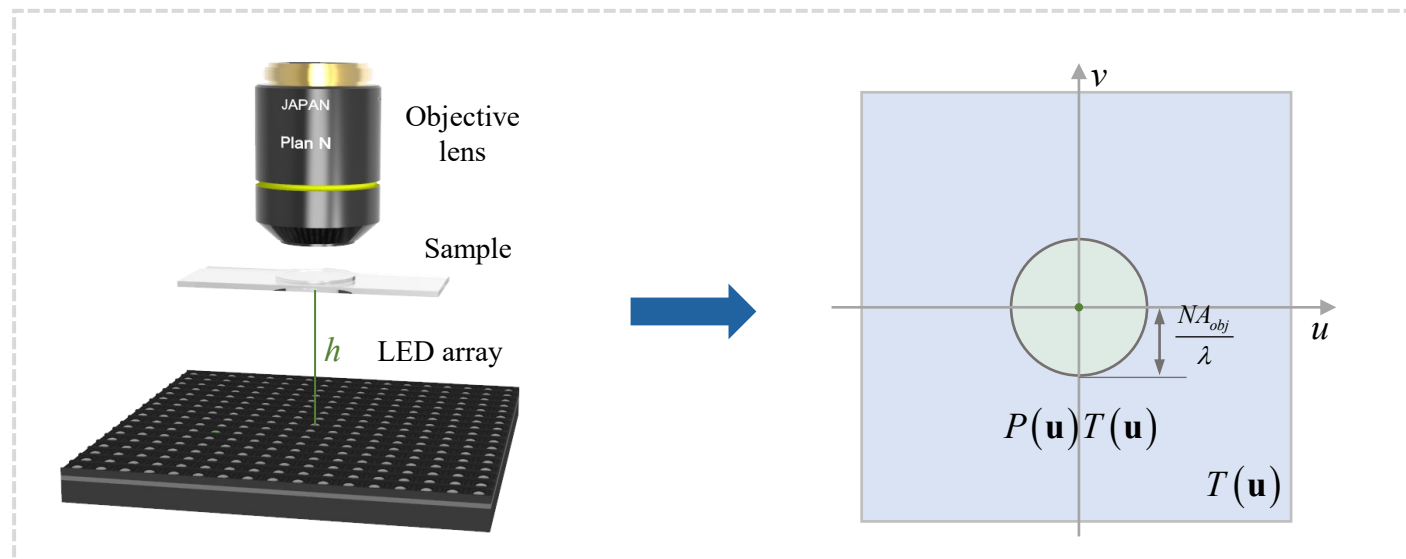
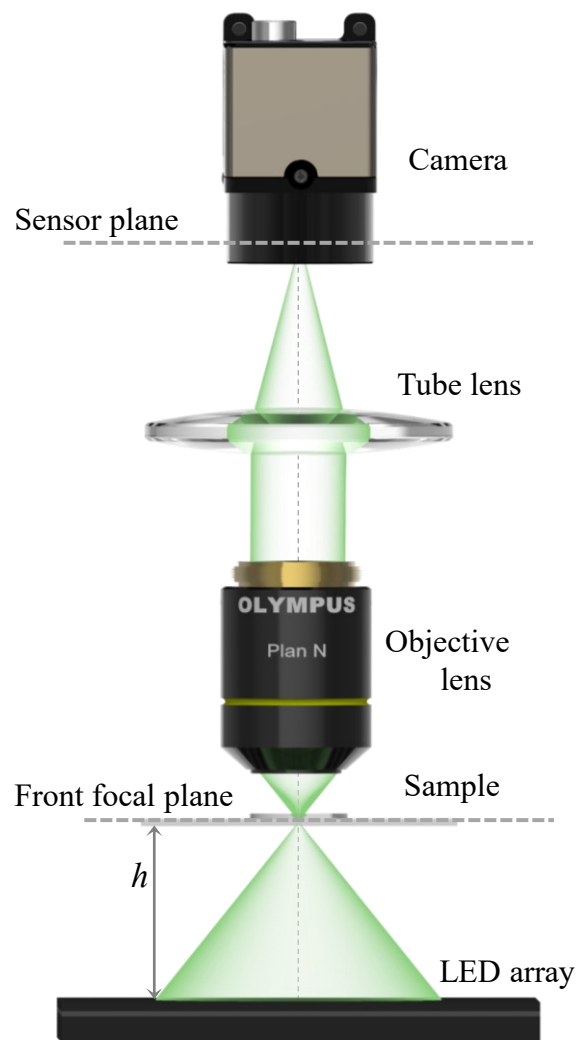
“所见即所得”

计算光学显微成像



	 Source	 Sample	 Imaging system	 Detector
Principle	Linear decomposition	Interaction Diffraction theory	Propagation or modulation	Intensity detection and sampling
Solution	Source points coherent modes	Scalar diffraction theory; Vector diffraction theory;	Linear systems theory	Amplitude square Non-coherent superposition
Analysis	Coherent properties	Superposition under plane-wave illumination	Linear spatially invariant system;	Time average
Model	Complex intensity; Wavelength; Coherence function; Spectrum distribution; Azimuth; Polarization	Complex transmittance function; Absorption function; Phase function; Refractive index; Polarization characteristics;	2D/3D coherent spread function 2D/3D point spread function; Coherent transfer function; Optical transfer function; 4D phase-space model;	Spectral response function; Quantum efficiency; Single Photon; Noise statistics; Modulation transfer function; Nonlinearity;
Modulation	Intensity; Phase; Angle; Aperture; Wavelength; Spatial coherence; Temporal coherence; Polarization; Paraxial approximation; etc.	Pure phase/weak object/ slowly varying approximations; Born or Rytvo approximation; Multi-slice propagation model; Non-negative refractive index approximation; etc.	Imaging aperture; Out-of-focus; Light deflection; Light intensity masks; Chromatic dispersion etc.	Controlled displacement: lateral and axial; Spectrum integration: spectrum response color cross-talk matrix; Pixelation effects: binning, downsampling, pixel response function, Bayer filter; Polarization detection; etc.

□ 倾斜照明



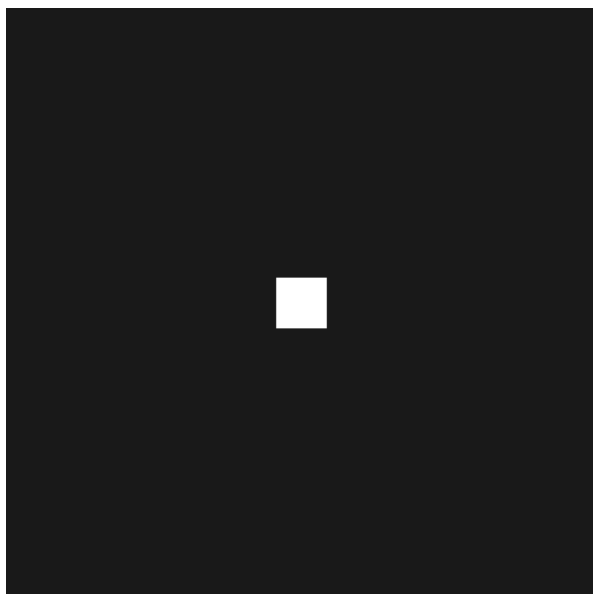
□ 倾斜照明

$$F\{w\} = F\{ae^{i\varphi}\} = W$$

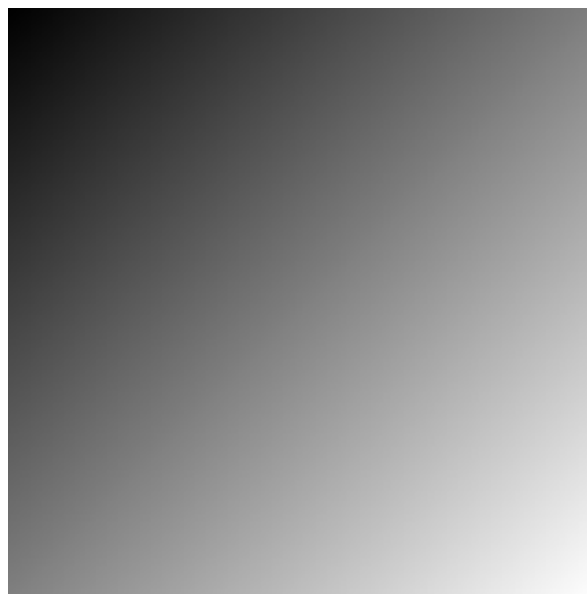
傅立叶变换对

$$F\{we^{i\theta}\} = F\{ae^{i\varphi}e^{i\theta}\} = W(u - k_x, v - k_y)$$

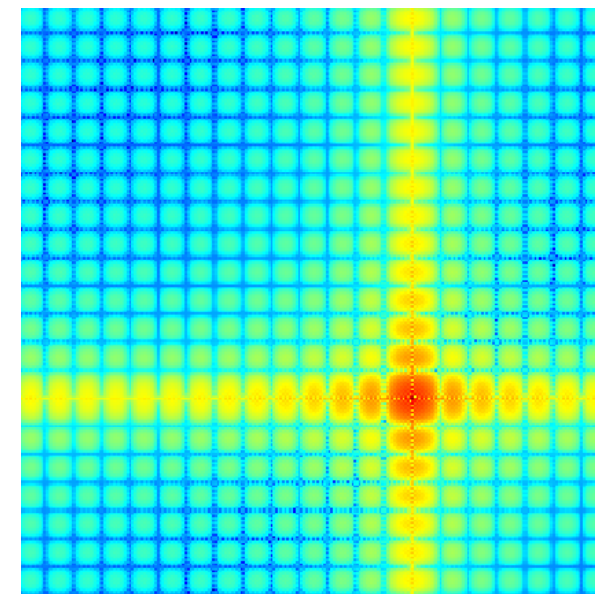
a



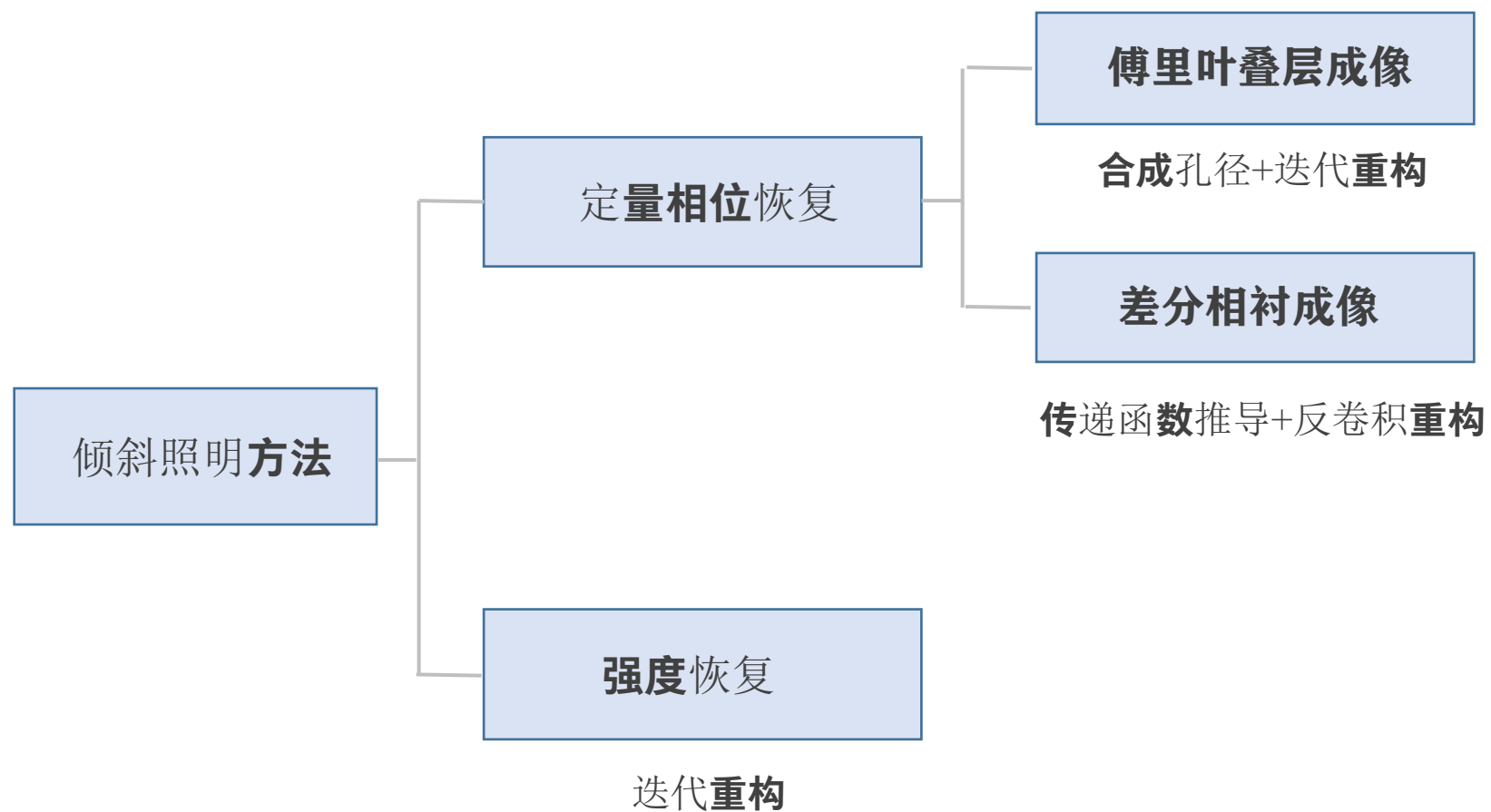
$\varphi + \theta$



$W(u - k_x, v - k_y)$



□ 倾斜照明



□ 部分相干成像系统图像生成模型

强度分布:

$$I(\mathbf{x}) = \iiint S(\mathbf{u}) \hat{T}(\mathbf{u}_1) \hat{T}^*(\mathbf{u}_2) H(\mathbf{u} + \mathbf{u}_1) H^*(\mathbf{u} + \mathbf{u}_2) e^{j2\pi\mathbf{x}(\mathbf{u}_1 - \mathbf{u}_2)} d\mathbf{u}_1 d\mathbf{u}_2 d\mathbf{u}$$

分离与样品无关的系统项:

$$I(\mathbf{x}) = \iint \hat{T}(\mathbf{u}_1) \hat{T}^*(\mathbf{u}_2) TCC(\mathbf{u}_1, \mathbf{u}_2) e^{j2\pi\mathbf{x}(\mathbf{u}_1 - \mathbf{u}_2)} d\mathbf{u}_1 d\mathbf{u}_2$$

部分相干传递函数/交叉传递系数

$$C(\mathbf{u}_1, \mathbf{u}_2) = \iint S(\mathbf{u}) H(\mathbf{u} + \mathbf{u}_1) H^*(\mathbf{u} + \mathbf{u}_2) d\mathbf{u}$$

□ 部分相干成像系统图像生成模型

$$I(\mathbf{x}) = \iiint S(\mathbf{u}) \hat{T}(\mathbf{u}_1) \hat{T}^*(\mathbf{u}_2) H(\mathbf{u} + \mathbf{u}_1) H^*(\mathbf{u} + \mathbf{u}_2) e^{j2\pi\mathbf{x}(\mathbf{u}_1 - \mathbf{u}_2)} d\mathbf{u}_1 d\mathbf{u}_2 d\mathbf{u}$$

1. 弱物体近似

$$t(x) = 1 + a(x) + i\phi(x)$$

$$I(x) = C(0,0) + 2 \operatorname{Re} \left\{ \int C(\mathbf{u},0) [a(\mathbf{u}) + j\phi(\mathbf{u})] e^{j2\pi\mathbf{x}\mathbf{u}} d\mathbf{u} \right\}$$

$$I(x) = C(0,0) + 2 \operatorname{Re} \left\{ \mathcal{F}^{-1} [A(\mathbf{u})a(\mathbf{u}) + jP(\mathbf{u})\phi(\mathbf{u})] \right\}$$

$A(\mathbf{u})$ 振幅传递函数

$P(\mathbf{u})$ 相位传递函数

2. 缓变物体近似

$$t(x) = e^{j\phi'(x)}$$

$$I(\mathbf{x}) = a^2 C \left(\frac{\phi'}{2\pi}, \frac{\phi'}{2\pi} \right)$$

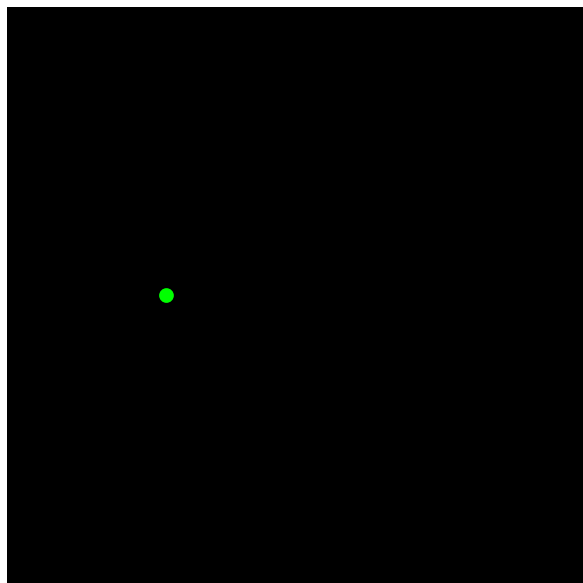
$C(\mathbf{u}, \mathbf{u})$ 相位梯度传递函数

□ 弱物体近似

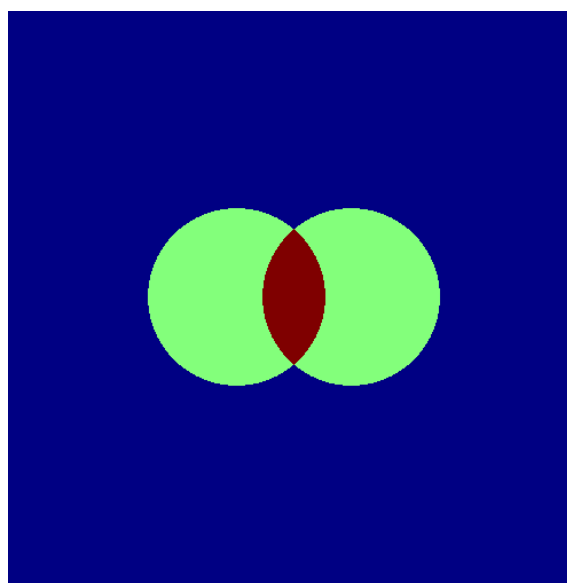
$$A(\mathbf{u}) = \iint S(\mathbf{u}') P^*(\mathbf{u}') P(\mathbf{u} + \mathbf{u}') d\mathbf{u}' + \iint S(\mathbf{u}') P(\mathbf{u}') P^*(\mathbf{u} - \mathbf{u}') d\mathbf{u}'$$

$$P(\mathbf{u}) = \iint S(\mathbf{u}') P^*(\mathbf{u}') P(\mathbf{u} + \mathbf{u}') d\mathbf{u}' - \iint S(\mathbf{u}') P(\mathbf{u}') P^*(\mathbf{u} - \mathbf{u}') d\mathbf{u}'$$

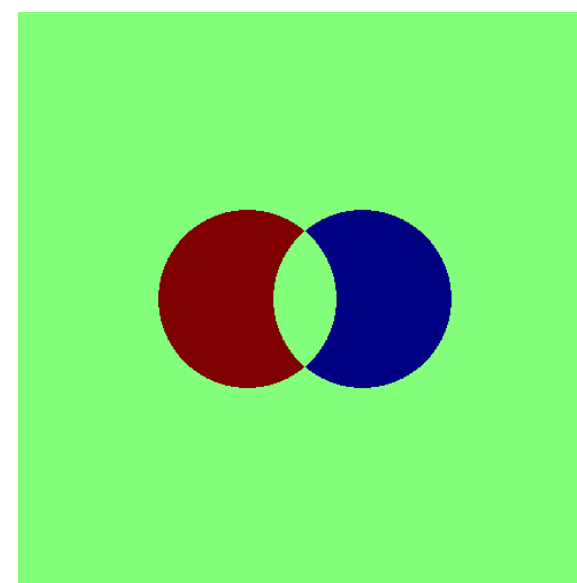
单点倾斜照明



振幅传递函数



相位传递函数



□ 弱物体近似下的定量相位求解

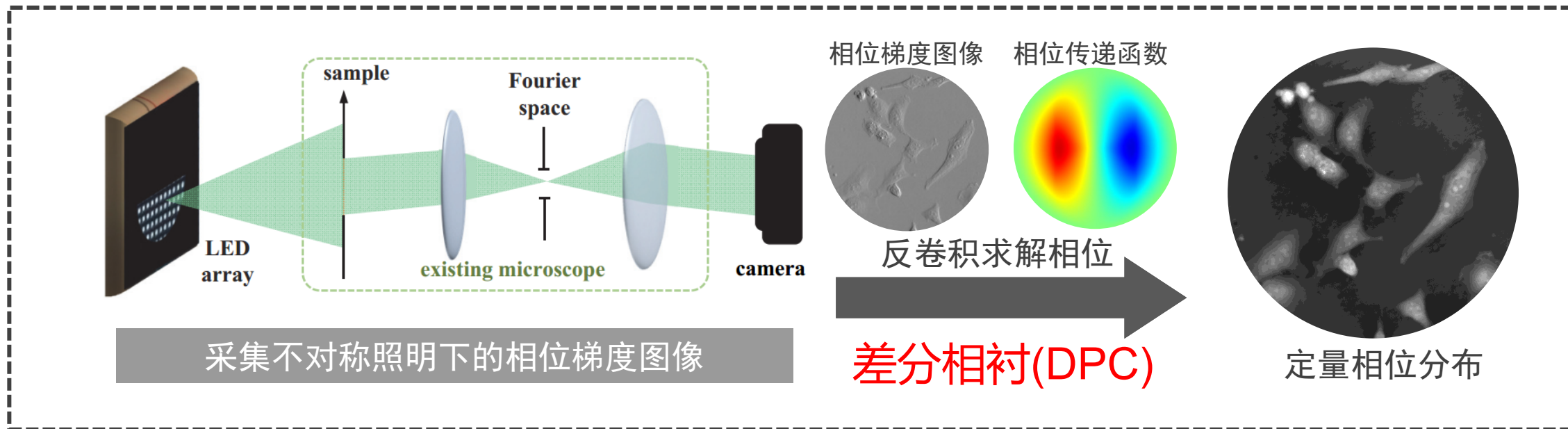
$$I(x) = B\delta(\mathbf{u}) + A(\mathbf{u})a(\mathbf{u}) + jP(\mathbf{u})\phi(\mathbf{u})$$

消去背景项和吸收项

$$I_{DPC} = \frac{I_L(x) - I_R(x)}{I_L(x) + I_R(x)}$$

反卷积求解:

$$\phi = \mathcal{F}^{-1} \left\{ \frac{\sum P_j^*(\mathbf{u}) I_{DPC,j}(\mathbf{u})}{\sum |P_j(\mathbf{u})|^2 + \alpha} \right\}$$



□ 缓变物体近似

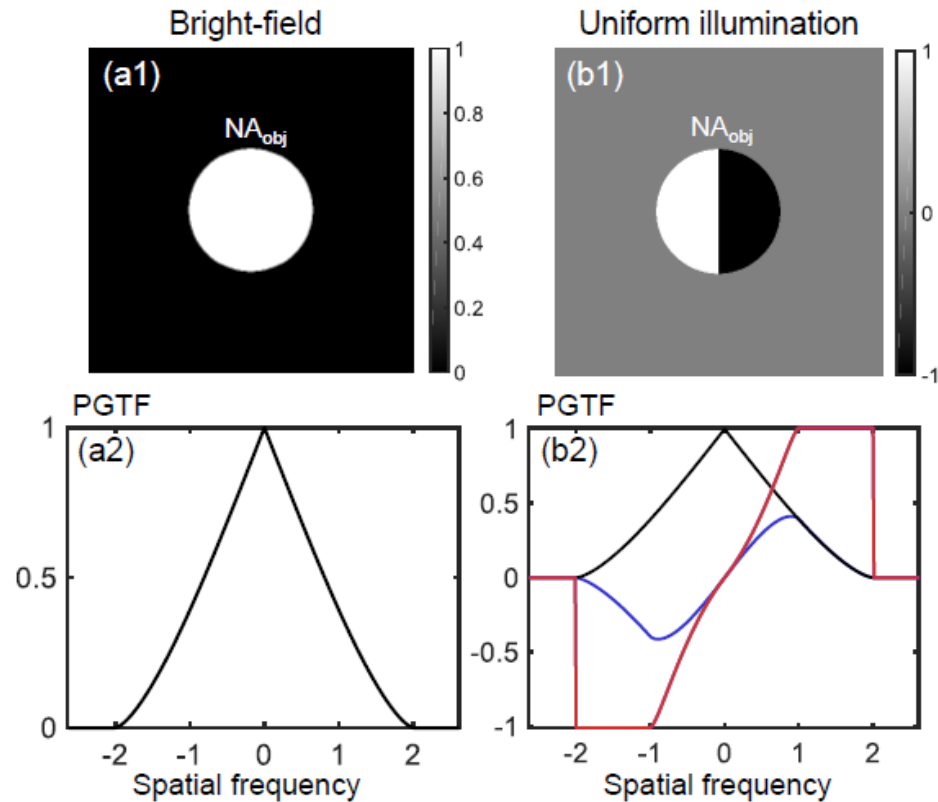
$$I(\mathbf{x}) = a^2 C\left(\frac{\phi'}{2\pi}, \frac{\phi'}{2\pi}\right)$$

相位梯度传递函数

$$PGTH = C(\mathbf{u}, \mathbf{u}) = \int S(\mathbf{u}' - \mathbf{u}) |P(\mathbf{u}')|^2 d\mathbf{u}'$$

相位梯度积分

$$\phi = \text{Im} \left[\mathcal{F}^{-1} \begin{cases} \frac{\mathcal{F} \{ \phi'_x + \phi'_y \}}{2\pi(u + iv)}, & |\mathbf{u}| \neq 0 \\ C, & |\mathbf{u}| = 0 \end{cases} \right]$$



扫描式差分相衬成像系统

Journal of Microscopy, Vol. 133, Pt 1, January 1984, pp. 27–39.
Received 1 November 1982; accepted 29 March 1983

Differential phase contrast in scanning optical microscopy

by D. K. HAMILTON and C. J. R. SHEPPARD, *University of Oxford, Department of Engineering Science, Parks Road, Oxford OX1 3P**

KEY WORDS. Scanning optical microscopy, differential interference contrast, Nomarski optics, laser, biological specimens, image formation, high resolution, optical microscopy.

SUMMARY

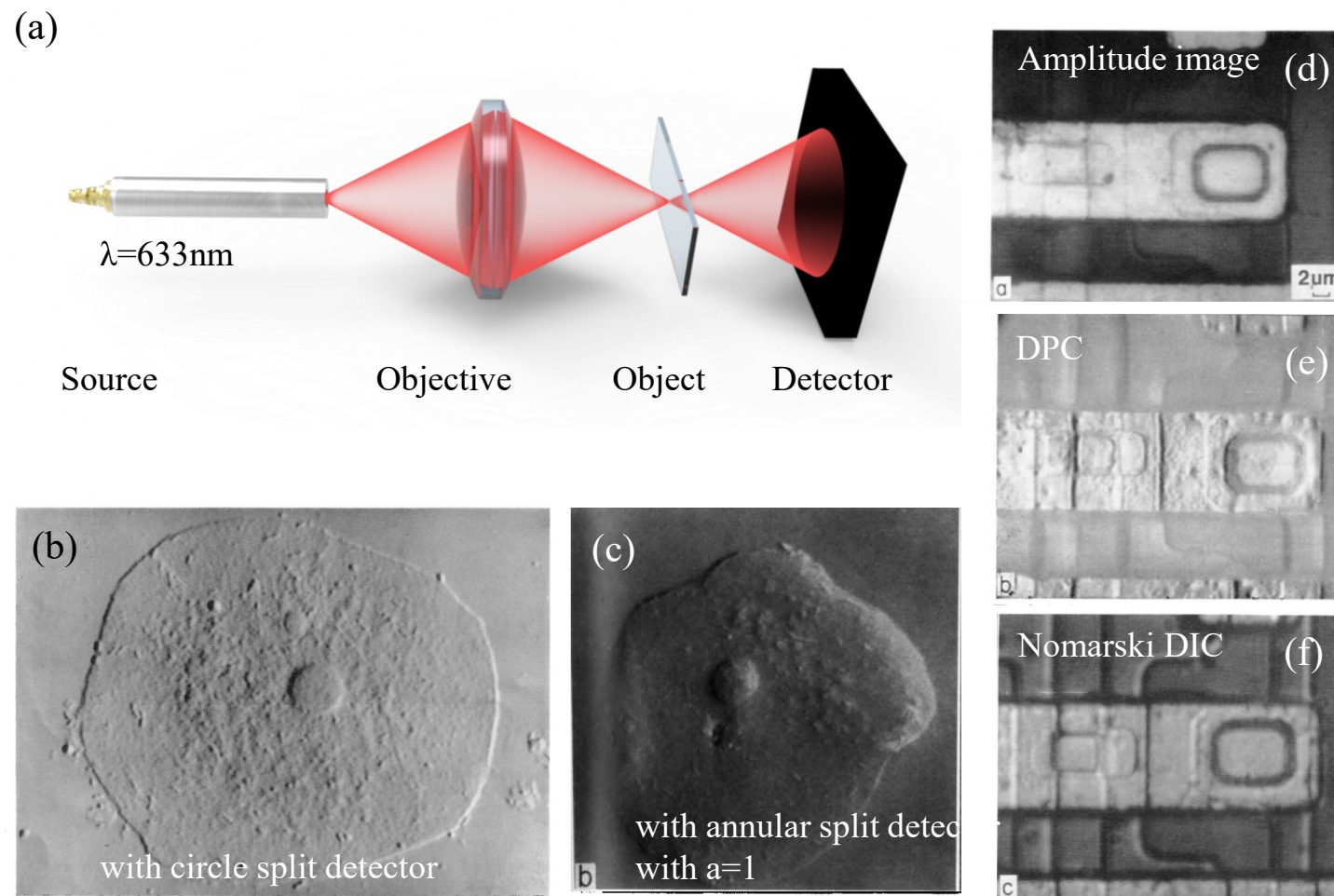
High-quality high-resolution transmission and reflection images produced using a scanning optical microscope and the split-detector technique are presented. These images exhibit differential phase contrast, the method avoiding some drawbacks of the usual Nomarski DIC arrangement. Imaging is treated theoretically and compared with the Nomarski method.

1. INTRODUCTION

Although Nomarski differential interference contrast (Nomarski, 1955) has become a widely used and powerful technique in optical microscopy it does have a number of disadvantages. A compromise must be made between contrast and signal level so that for objects with weak variations the signal may be very weak and in order to obtain adequate contrast the condenser must often be stepped down somewhat so that optimum resolution is no longer achieved. In general the image is formed by a complicated mixture of different contrast mechanisms including non-differential amplitude and differential amplitude contrast and with birefringent specimens it must be used with care.

A method widely used for scanning transmission electron microscopy (Dekkers & de Lang, 1974, 1977) based on a split detector, overcomes these problems, and indeed its use in scanning optical microscopy was suggested in the paper in which it was originally described (Dekkers & de Lang, 1974). However, until now, production of high-quality high-resolution optical images using the technique has not been reported.

Hamilton, D. K., & Sheppard, C. J. R. (1984).



全场差分相衬成像系统

1924 OPTICS LETTERS / Vol. 34, No. 13 / July 1, 2009

Quantitative phase-gradient imaging at high resolution with asymmetric illumination-based differential phase contrast

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Received March 30, 2009; revised May 22, 2009; accepted May 24, 2009; posted May 27, 2009 (Doc. ID 109303); published June 18, 2009

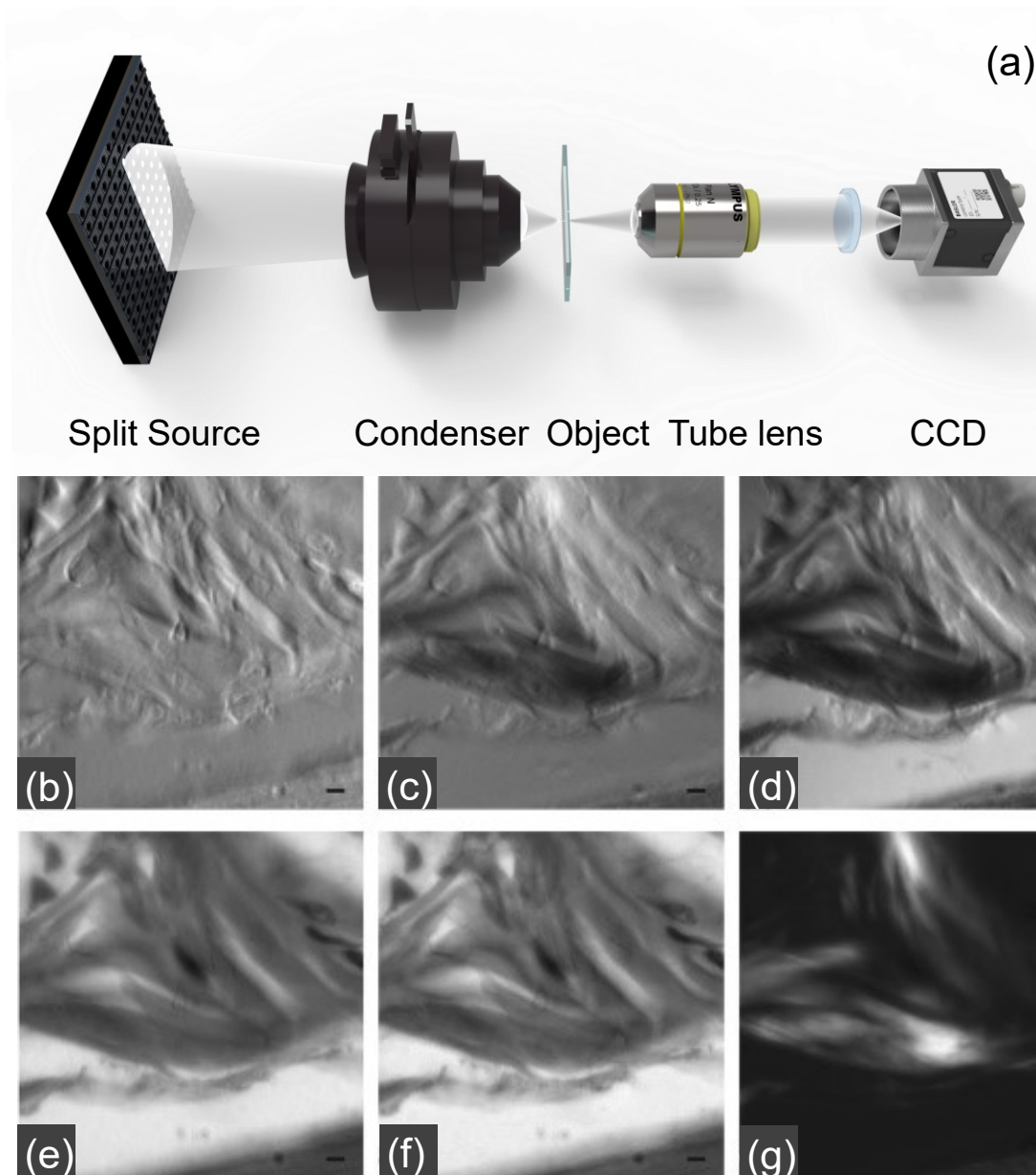
We describe a full-field phase-gradient imaging method: asymmetric illumination-based differential phase contrast (AIDPC). Imaging properties of AIDPC are evaluated using the phase-gradient transfer-function approach and elucidated with experimental images of an optical fiber and a histochemical preparation of a skeletal muscle section. In comparison with full-field differential interference contrast, AIDPC does not require phase shifting for quantitative imaging of phase gradient, provides artifact-free images of birefringent specimens, requires shorter camera exposure, and has larger depth of focus. It is amenable to transfer-function engineering, simultaneous fluorescence imaging, and automated live cell imaging. © 2009 Optical Society of America

OCIS codes: 110.0180, 110.4850, 100.5070, 110.4980.

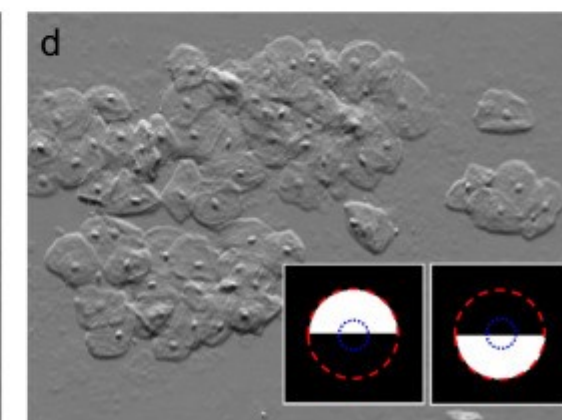
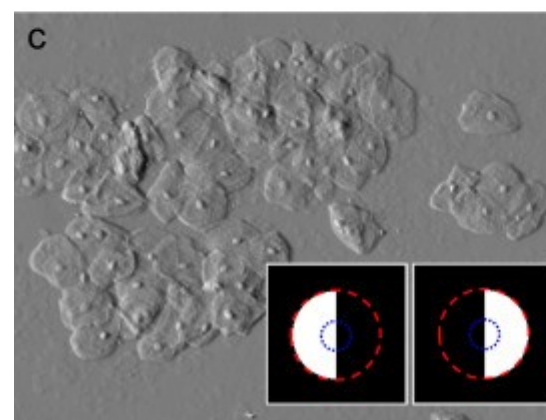
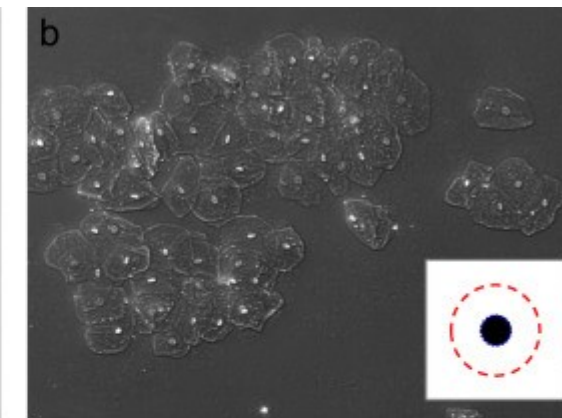
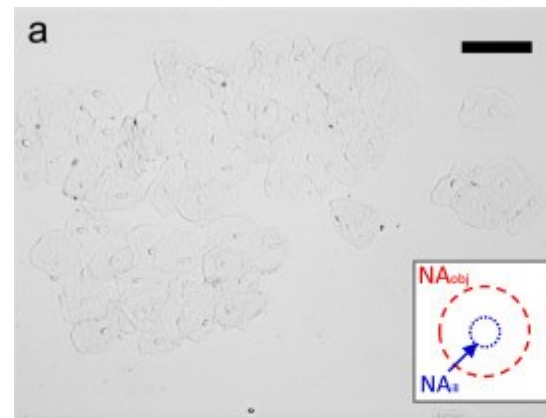
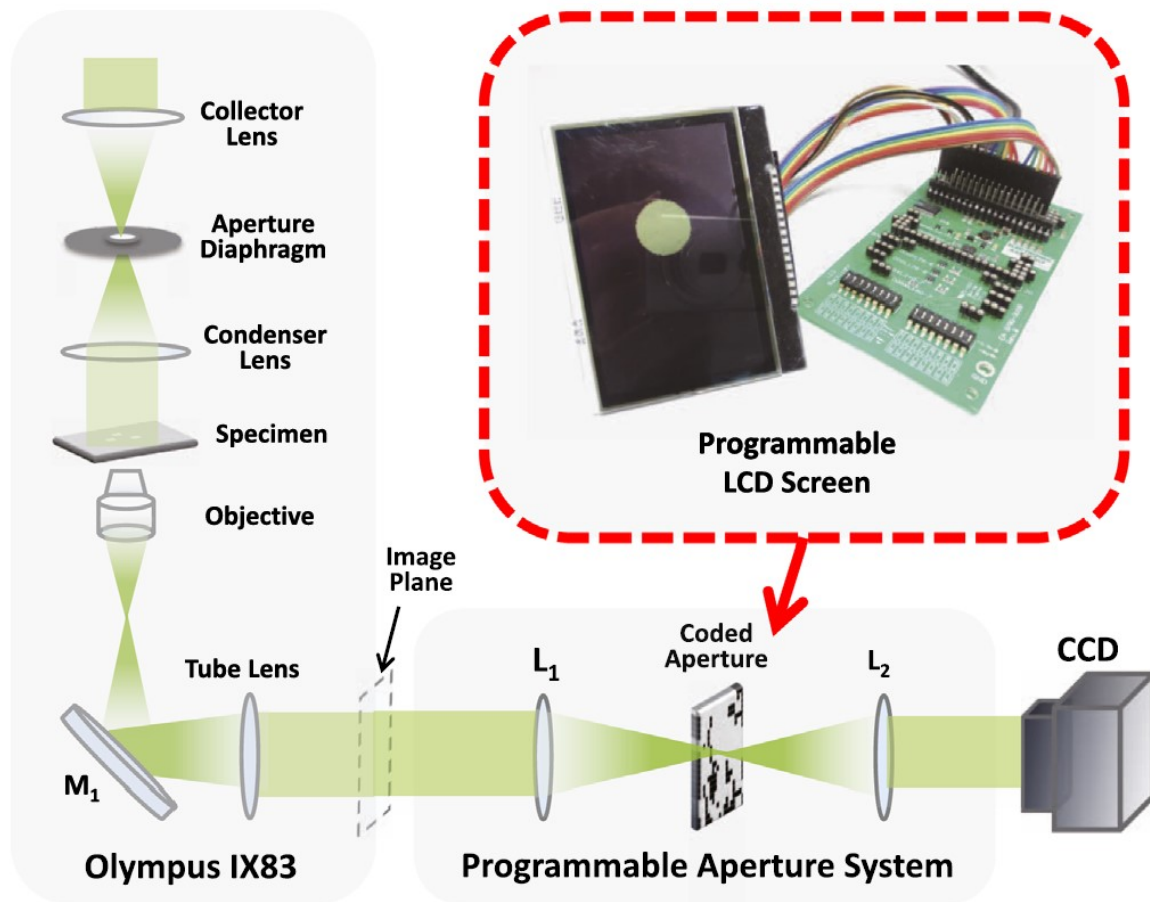
Imaging of biological specimens requires special optical processing to translate the optical thickness (i.e., phase) information to image intensity. Direct quantitative measurement of phase requires use of coherent illumination, leading to limited spatial resolution, lack of optical sectioning, and speckle from imperfections in the optical train. Phase-gradient imaging methods such as Nomarski's differential interference contrast (DIC) can accommodate large illumination apertures (i.e., partially coherent illumination), alleviating the above problems. In scanning optical microscopy, an intrinsically linear phase-gradient contrast method, termed differential phase contrast (DPC) has been evaluated [1–3]. In contrast to DPC, DIC images a complex mix of amplitude and phase-gradient information, necessitating approaches such as phase shifting (PSDIC) to establish a linear rela-

tional to those of the full-field system with an incoherent source if two conditions are met [11]: (1) each system has the same objective apertures (i.e., pupil amplitude), $P_o(\xi, \eta)$ and (2) the sensitivity distribution of the detector in the scanning system is the same as the intensity distribution of the condenser aperture, $|P_c(\xi, \eta)|^2$, in the full-field system. In scanning DPC, a split-detector or a quadrant diode is placed in the Fourier plane of the collector, and the image is formed by subtracting intensities recorded by two halves of the detector. A reciprocal wide-field DPC system has an antisymmetric condenser aperture with half of the aperture having negative effective intensity. We synthesize negative condenser intensity by subtracting two images acquired with semicircular condenser apertures in the direction of differentiation

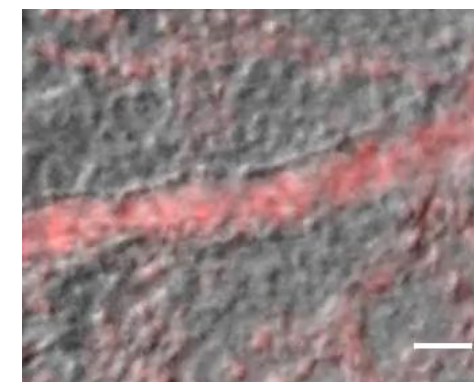
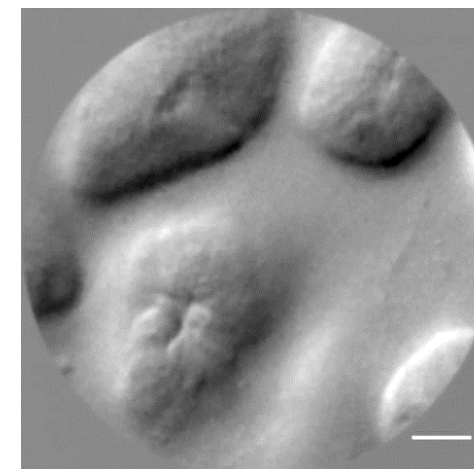
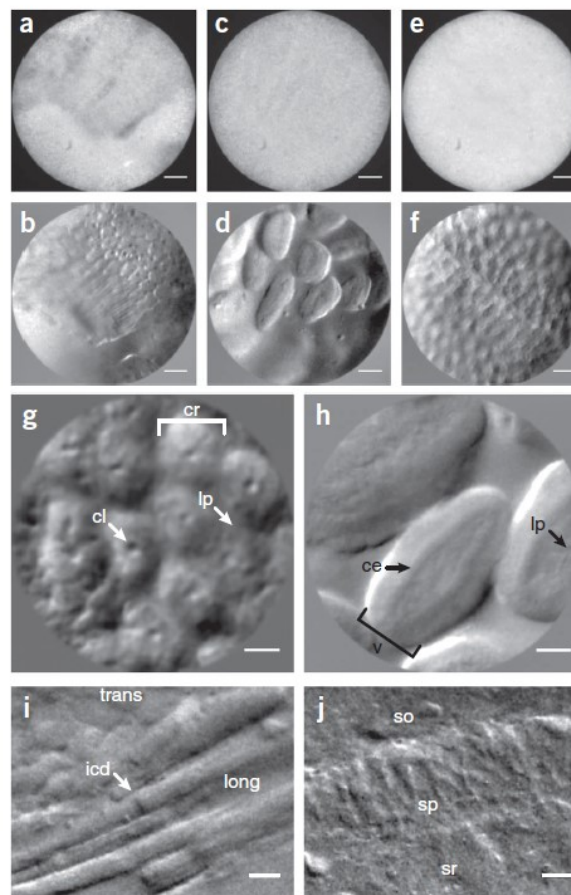
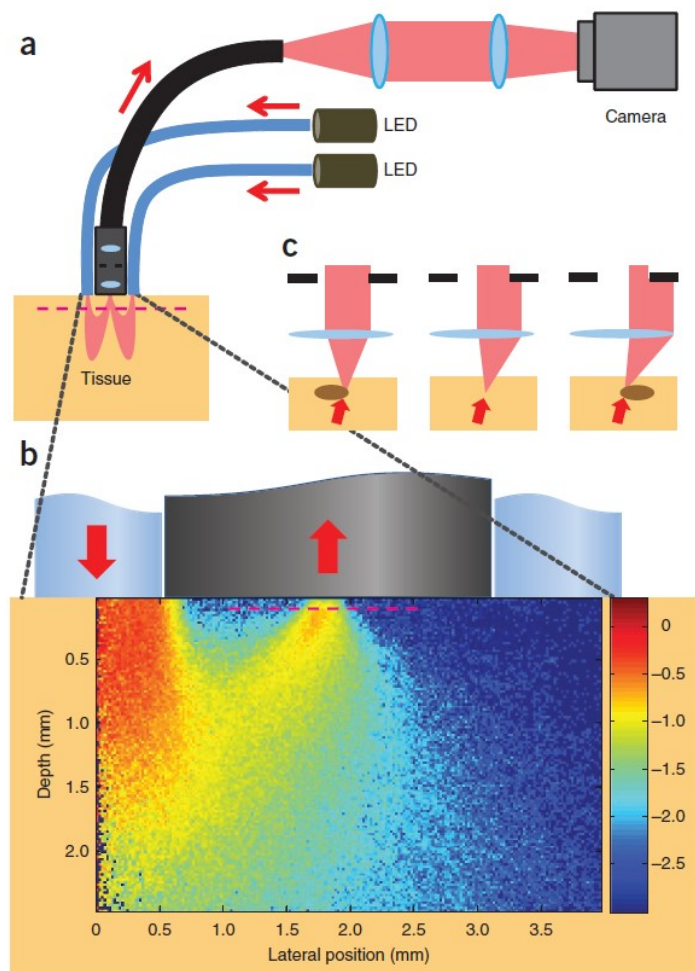
Mehta S. B. & Sheppard, C. J. R. (2009).



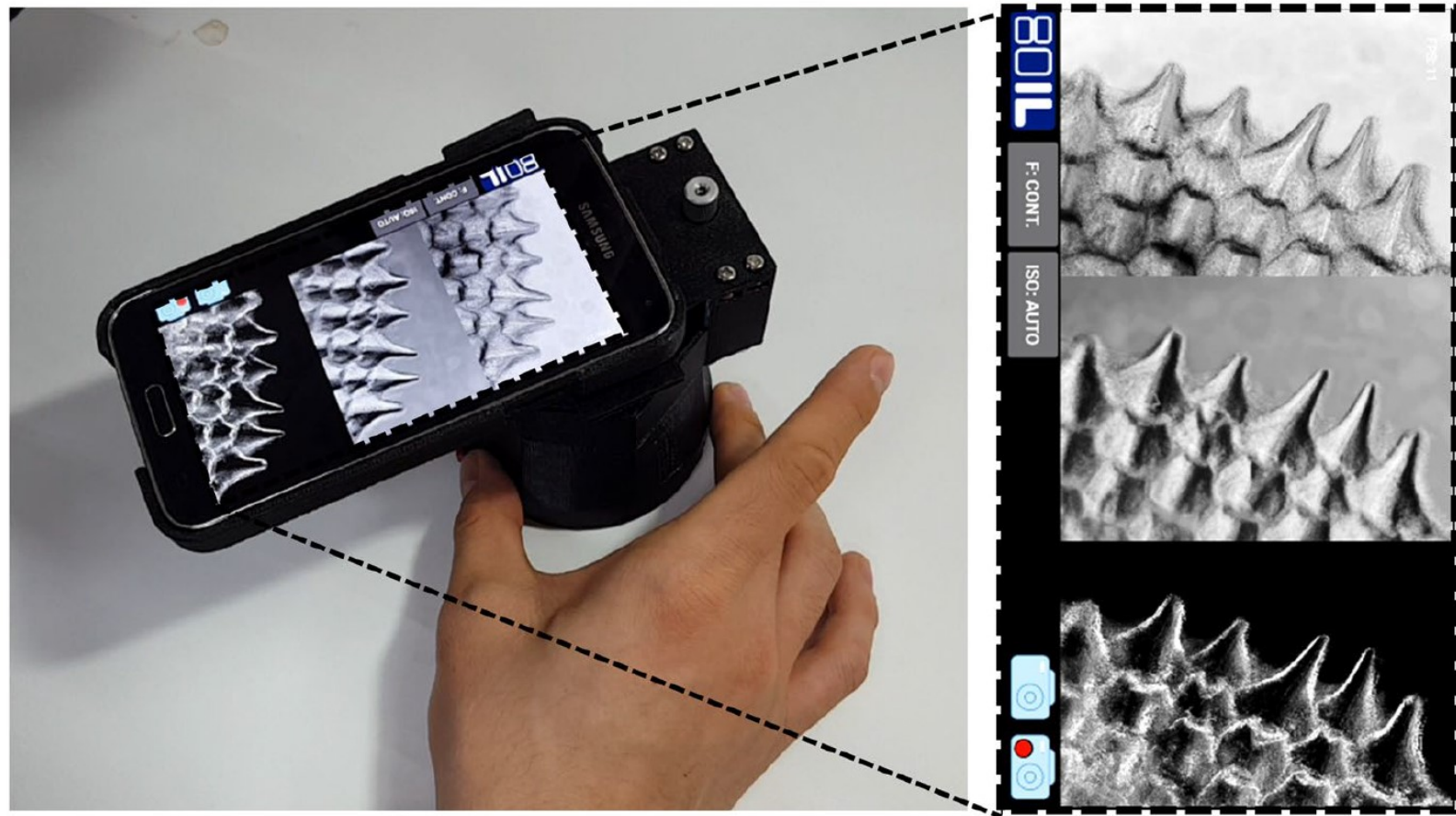
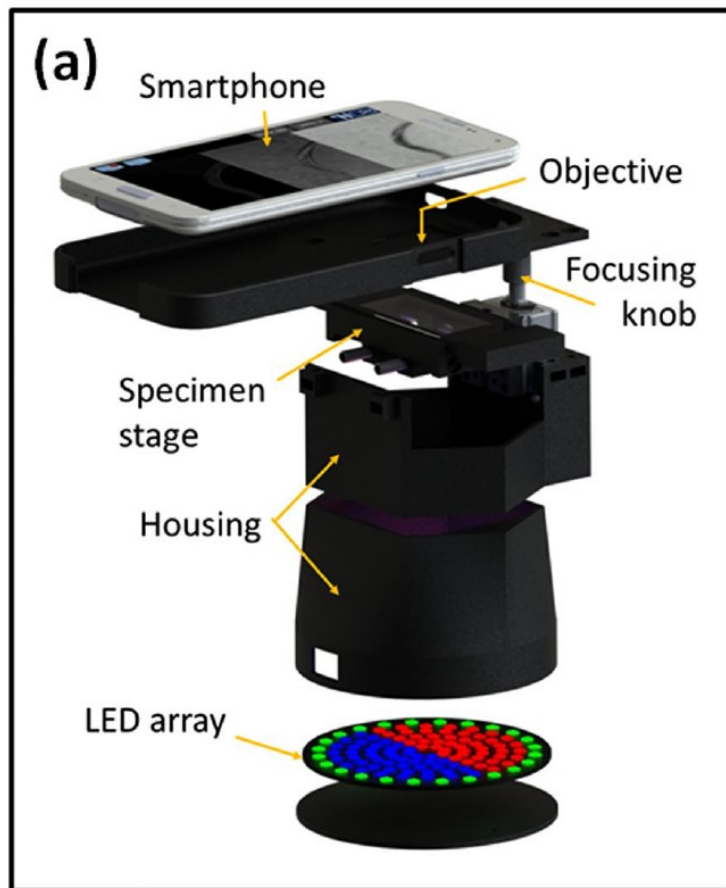
□ 基于LCD的可编程孔径差分相衬成像系统



□ 和内窥镜相结合，用于手术过程中成像



□ 结合智能手机，便携化差分相衬成像系统



Quantitative differential phase contrast imaging in an LED array microscope

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*lei.tian@alum.mit.edu

Abstract: Illumination-based differential phase contrast (DPC) is a phase imaging method that uses a pair of images with asymmetric illumination patterns. Distinct from coherent techniques, DPC relies on spatially partially coherent light, providing 2× better lateral resolution, better optical sectioning and immunity to speckle noise. In this paper, we derive the 2D weak object transfer function (WOTF) and develop a quantitative phase reconstruction method that is robust to noise. The effect of spatial coherence is studied experimentally, and multiple-angle DPC is shown to provide improved frequency coverage for more stable phase recovery. Our method uses an LED array microscope to achieve real-time (10 Hz) quantitative phase imaging with in vitro live cell samples.

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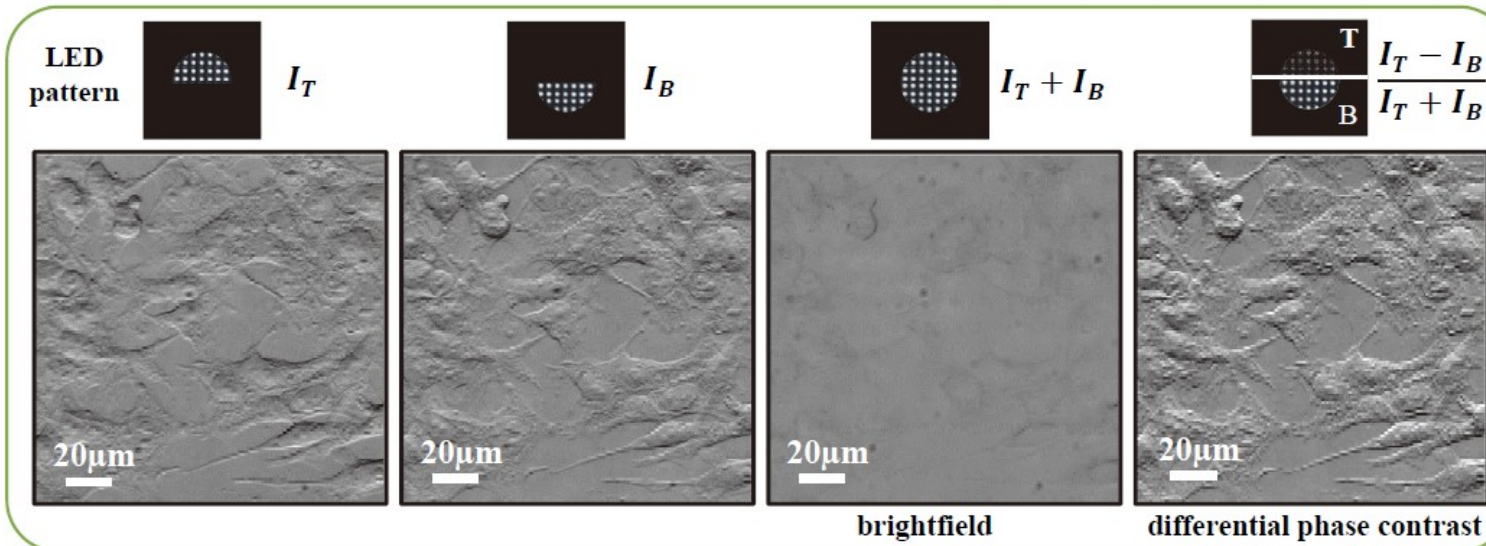
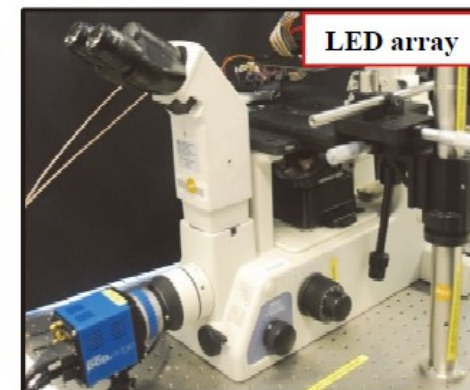
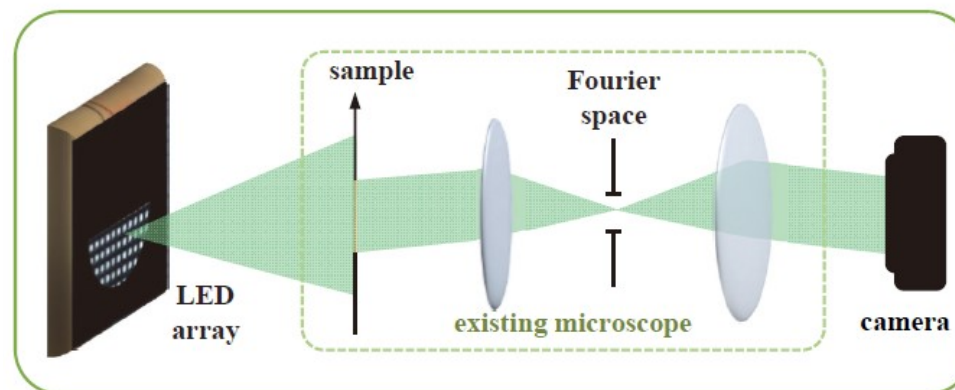
OCIS codes: (100.5070) Phase retrieval; (110.1758) Computational imaging; (170.0180) Microscopy; (110.3010) Image reconstruction techniques.

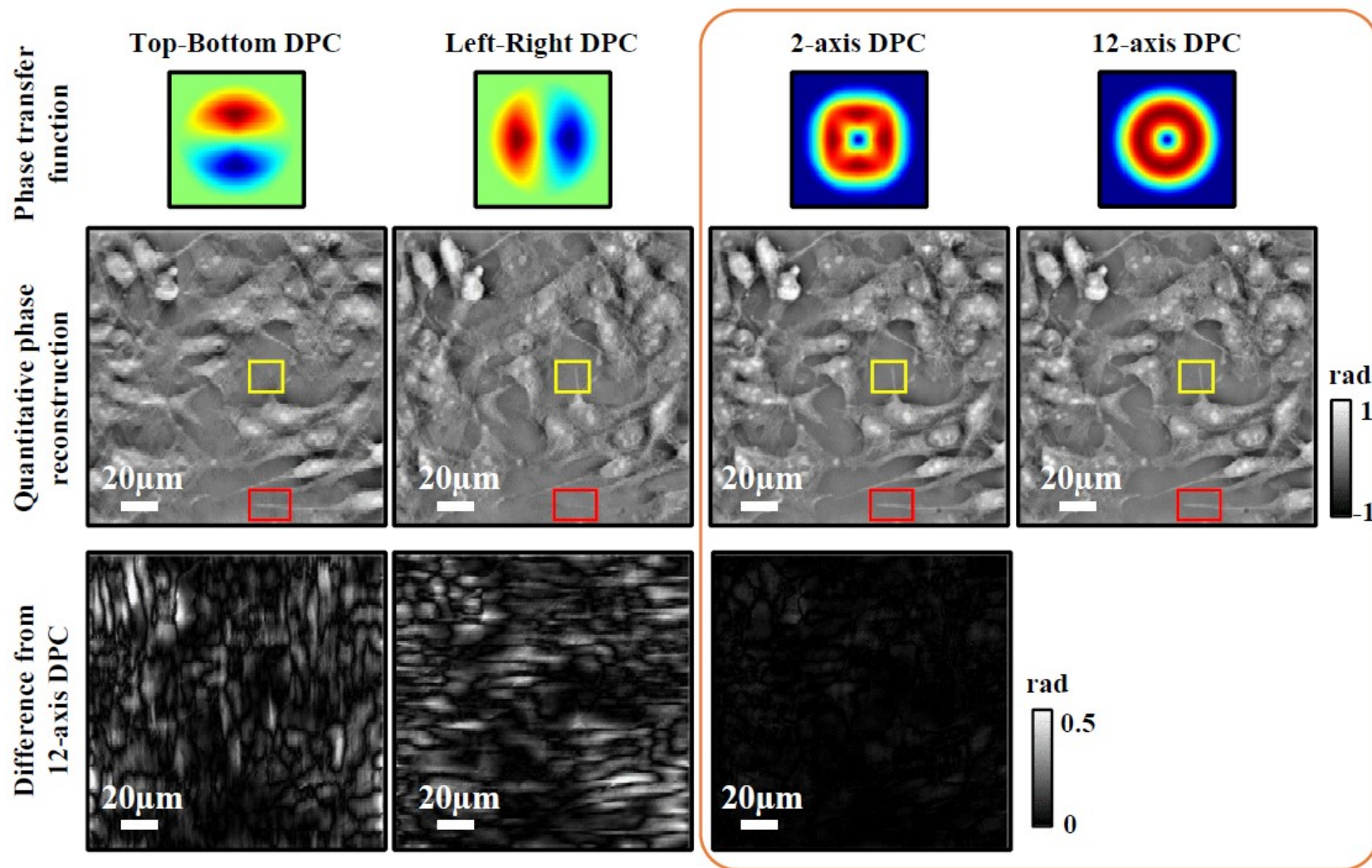
References and links

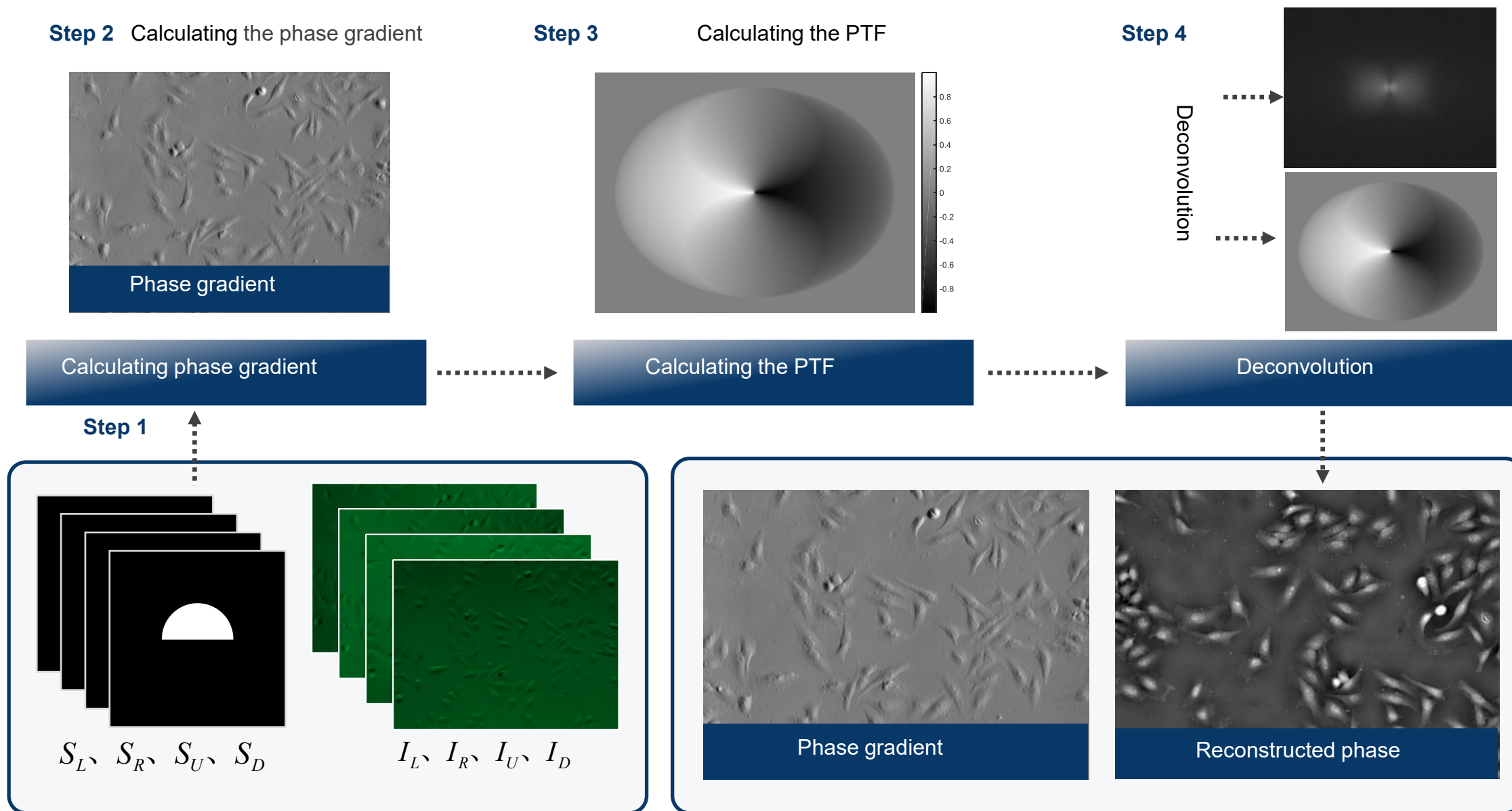
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2. M. R. Teague, "Deterministic phase retrieval: a Green's function solution," *J. Opt. Soc. Am.* **73**, 1434-1441 (1983).
3. N. Streibl, "Phase imaging by the transport equation of intensity," *Opt. Commun.* **49**, 6-10 (1984).
4. C. J. R. Sheppard, "Defocused transfer function for a partially coherent microscope and application to phase retrieval," *J. Opt. Soc. Am. A* **21**, 828-831 (2004).
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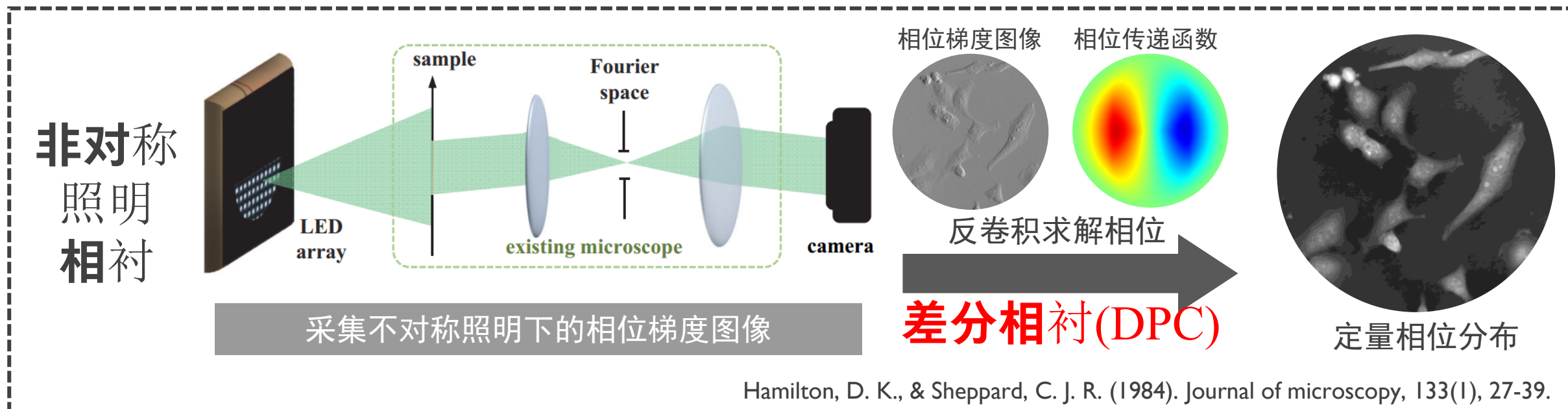
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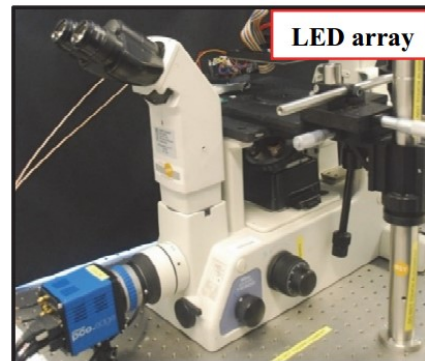
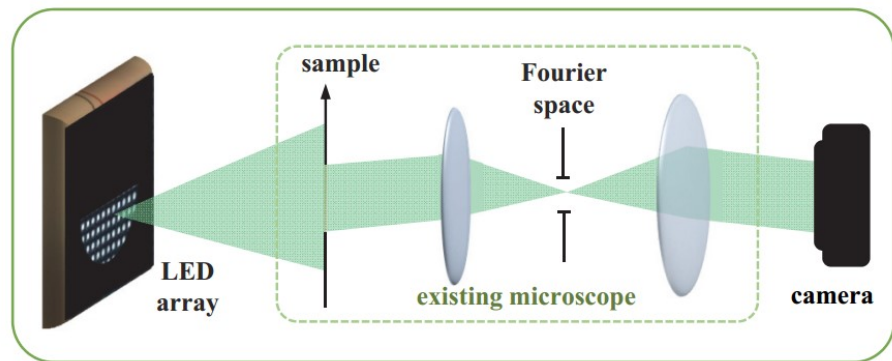






1. 探究成像机理，完善成像模型与算法
2. 提升成像分辨率，实现高分辨率成像
3. 发展快速定量相位成像技术，实现活细胞实时动态成像
4. 构建定量相位成像系统，针对专业化应用进行系统设计和开发

差分相衬定量相位成像

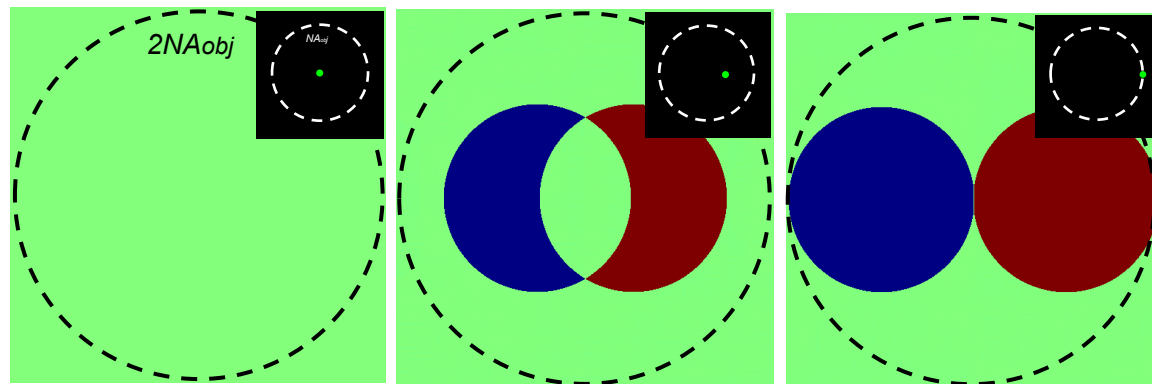


$$PTF(\mathbf{u}) = \frac{\iint S(\mathbf{u}_j)[P^*(\mathbf{u}_j)P(\mathbf{u} + \mathbf{u}_j) - P(\mathbf{u}_j)P^*(\mathbf{u} - \mathbf{u}_j)]d^2\mathbf{u}_j}{\iint S_l(\mathbf{u}_j)|P(\mathbf{u}_j)|^2 d^2\mathbf{u}_j}$$

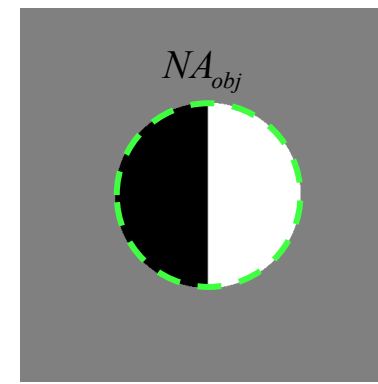
$PTF(\mathbf{u})$ 相位传递函数

$S(\mathbf{u})$ 照明函数 $P(\mathbf{u})$ 光瞳函数

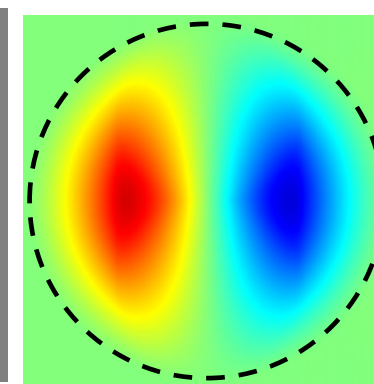
单点非对称照明的相位传递函数



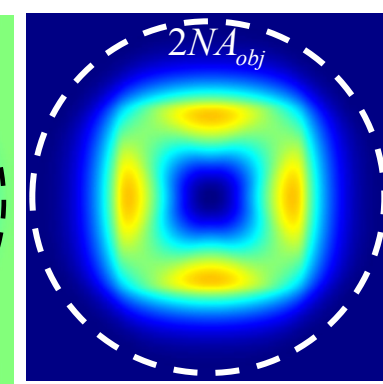
传统半圆形照明



左右PTF



合成PTF



- 频谱带宽受限，低频对比度差，无法恢复高分辨率细节
- 传递响应各向异性，成像分辨率各向异性

基于最优照明的差分相衬定量相位成像

$$PTF(\mathbf{u}) = \frac{\iint S(\mathbf{u}_j)[P^*(\mathbf{u}_j)P(\mathbf{u}+\mathbf{u}_j) - P(\mathbf{u}_j)P^*(\mathbf{u}-\mathbf{u}_j)]d^2\mathbf{u}_j}{\iint S_l(\mathbf{u}_j)|P(\mathbf{u}_j)|^2 d^2\mathbf{u}_j}$$

$PTF(\mathbf{u})$ 相位传递函数

$S(\mathbf{u})$ 照明函数 $P(\mathbf{u})$ 光瞳函数



极坐标相位传递函数建模

$$PTF_{lr}(\rho, \theta) = \begin{cases} \frac{2 \int_{\rho-NA_{obj}}^{NA_{obj}} \int_{\theta-\alpha}^{\theta+\alpha} S_{lr}(\xi, \varepsilon) d\varepsilon d\xi}{\int_0^{NA_{obj}} \int_0^{2\pi} |S_{lr}(\xi, \varepsilon)| d\varepsilon d\xi} & NA_{obj} \leq \rho \leq 2NA_{obj} \\ \frac{2 \int_{NA_{obj}-\rho}^{NA_{obj}} \int_{\theta-\alpha}^{\theta+\alpha} S_{lr}(\xi, \varepsilon) d\varepsilon d\xi}{\int_0^{NA_{obj}} \int_0^{2\pi} |S_{lr}(\xi, \varepsilon)| d\varepsilon d\xi} & 0 \leq \rho < NA_{obj} \end{cases}$$

$$NA_{obj} \leq \rho \leq 2NA_{obj}$$

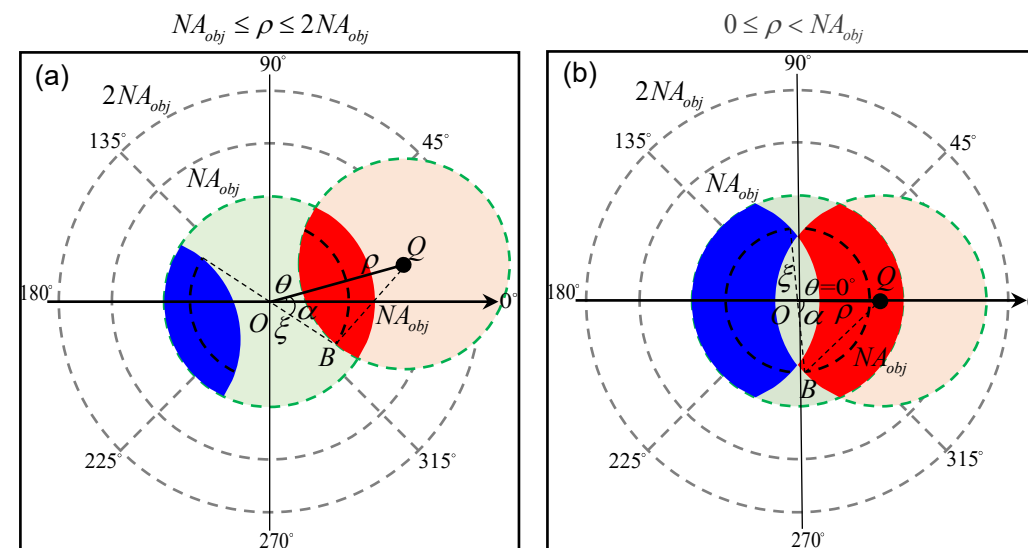
$$0 \leq \rho < NA_{obj}$$



广义各向同性
照明函数

$$S_{lr}(\rho, \theta) = L(\rho) \cos(n\theta)$$

$$S_{ud}(\rho, \theta) = L(\rho) \sin(n\theta)$$



基于最优照明的差分相衬定量相位成像

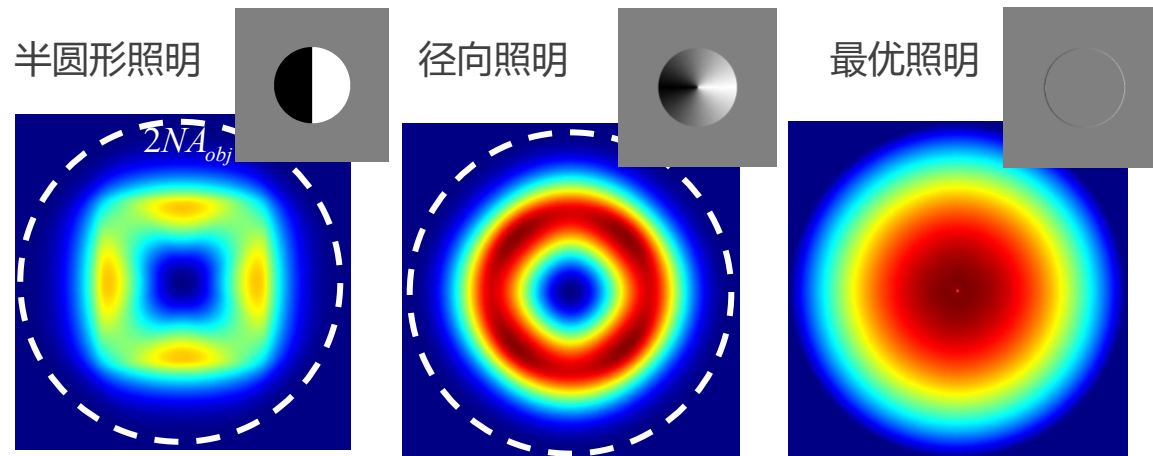
广义各向同性照明函数 \rightarrow

$$S_{lr}(\rho, \theta) = M(\rho) \cos(n\theta)$$

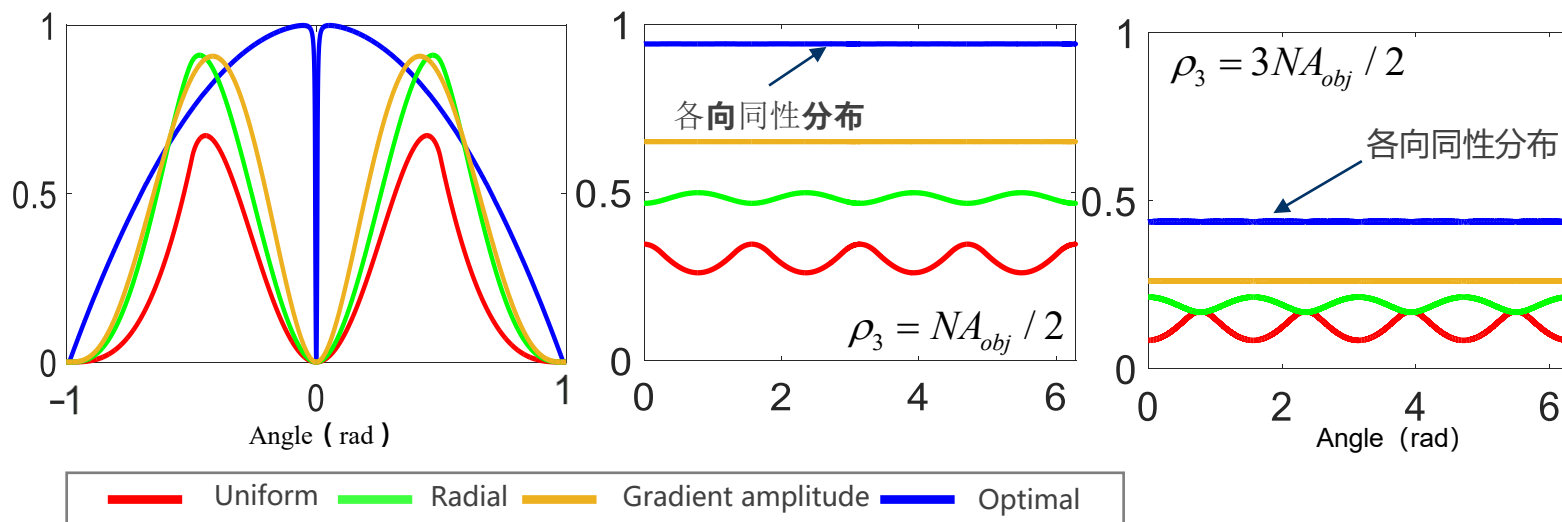
$$S_{ud}(\rho, \theta) = N(\rho) \sin(n\theta)$$

最优照明函数 \rightarrow

$$S_{lr}(\rho, \theta) = \delta(\rho - NA_{obj}) \cos(\theta)$$

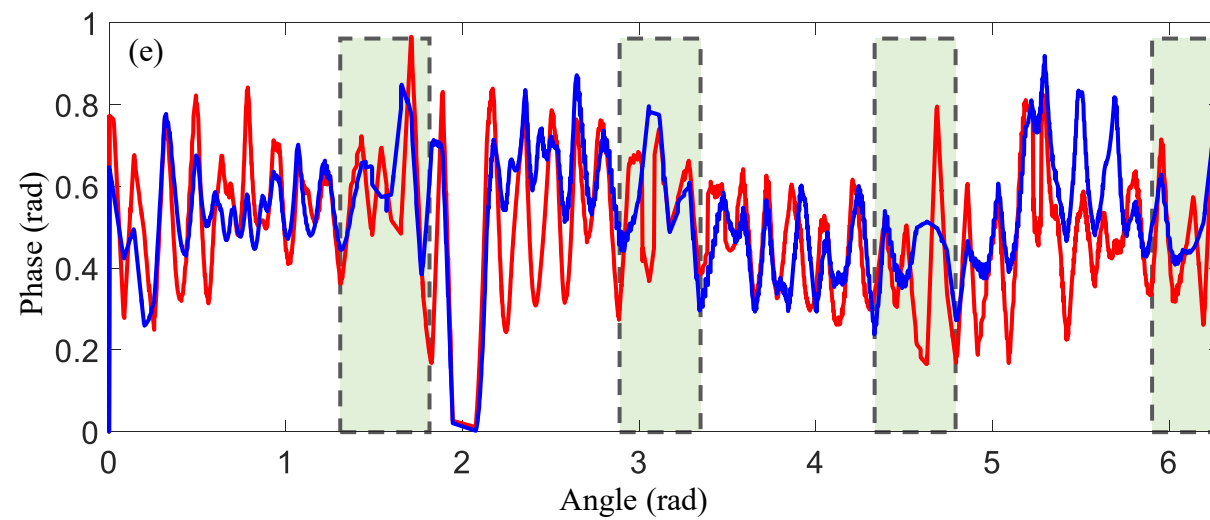
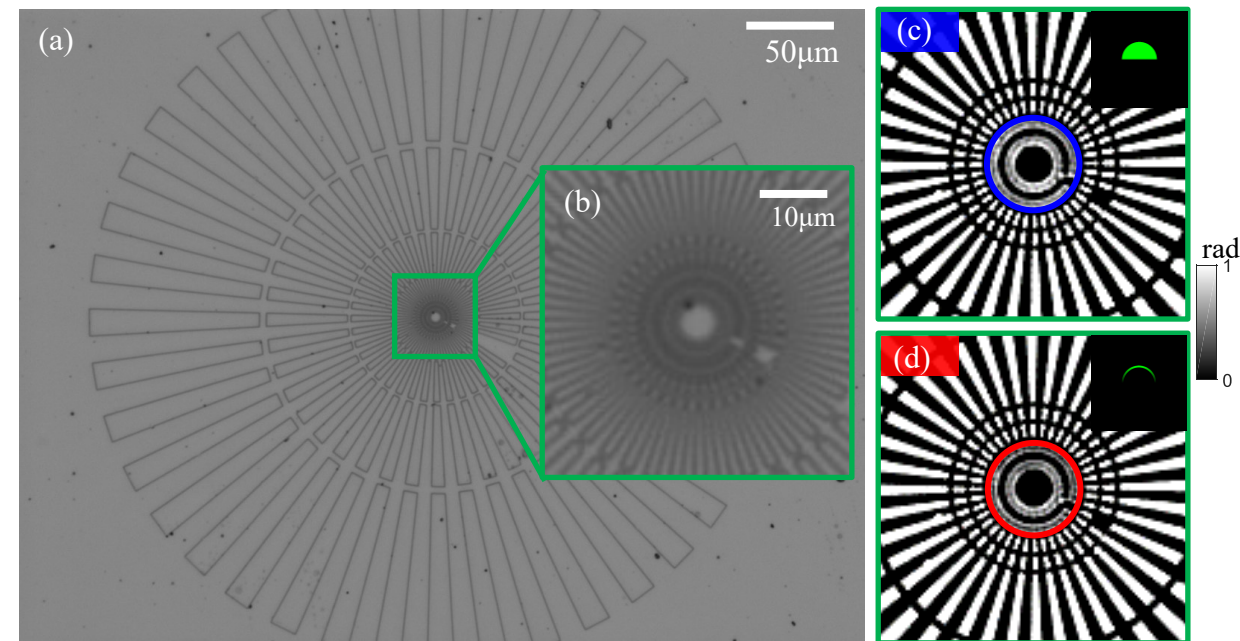
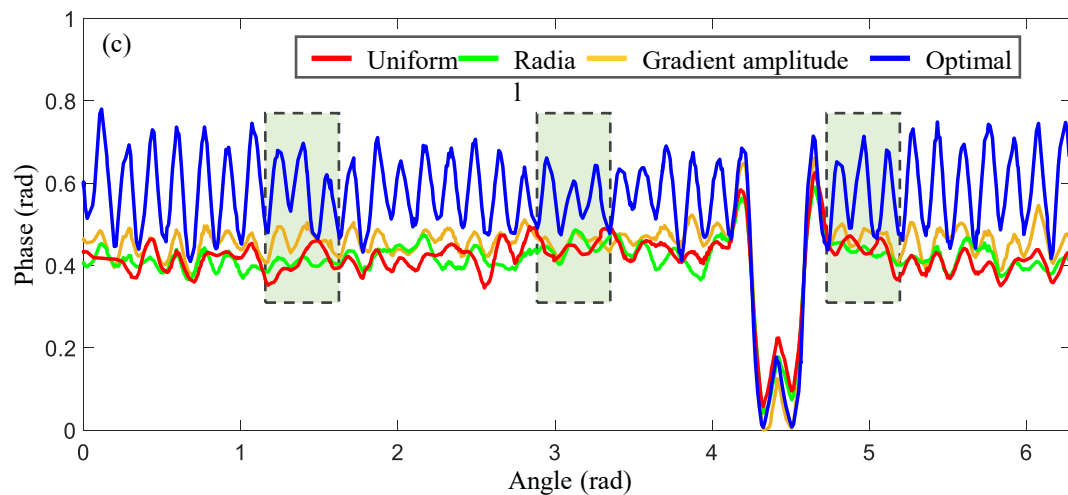
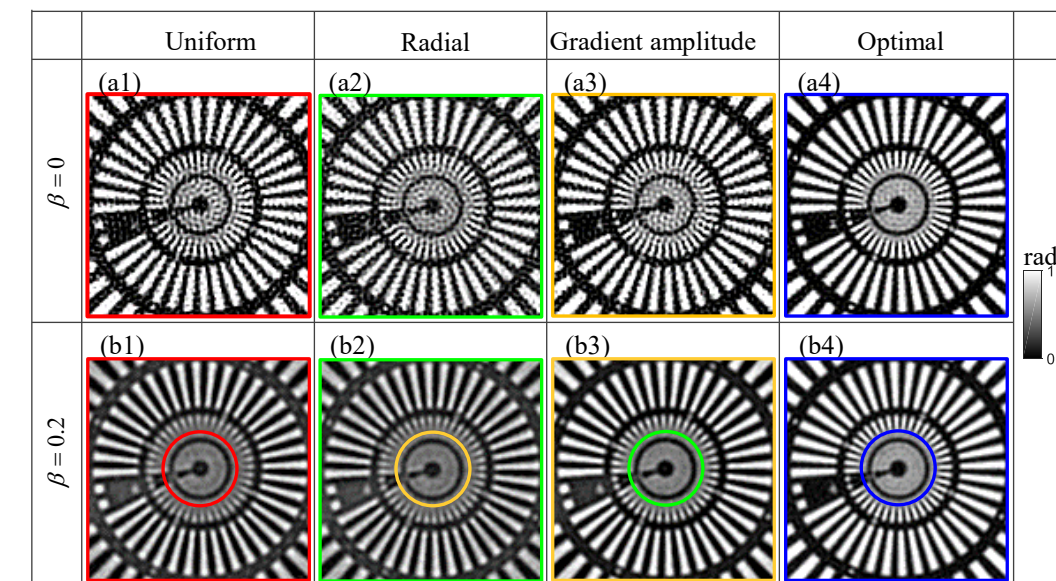
$$S_{ud}(\rho, \theta) = \delta(\rho - NA_{obj}) \sin(\theta)$$


传递函数剖面对比



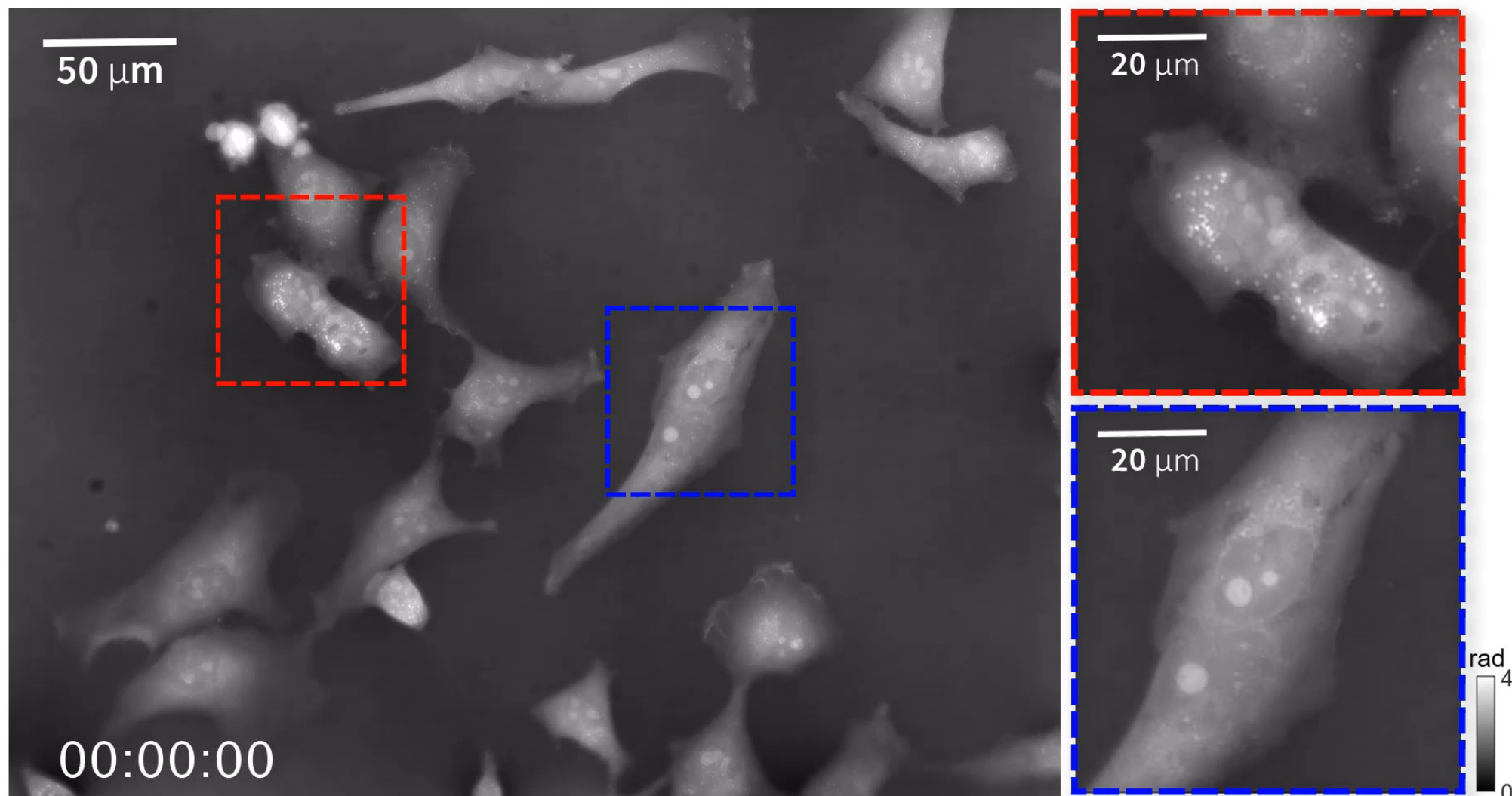
**传递响应在
全频谱带宽内增强
传递响应
数值分布各向同性**

基于最优照明的差分相衬定量相位成像



基于最优照明的差分相衬定量相位成像

Hela细胞5小时动态定量相位结果（每幅相位由4幅采集图像恢复）



基于彩色复用照明的单帧差分相衬定量相位成像

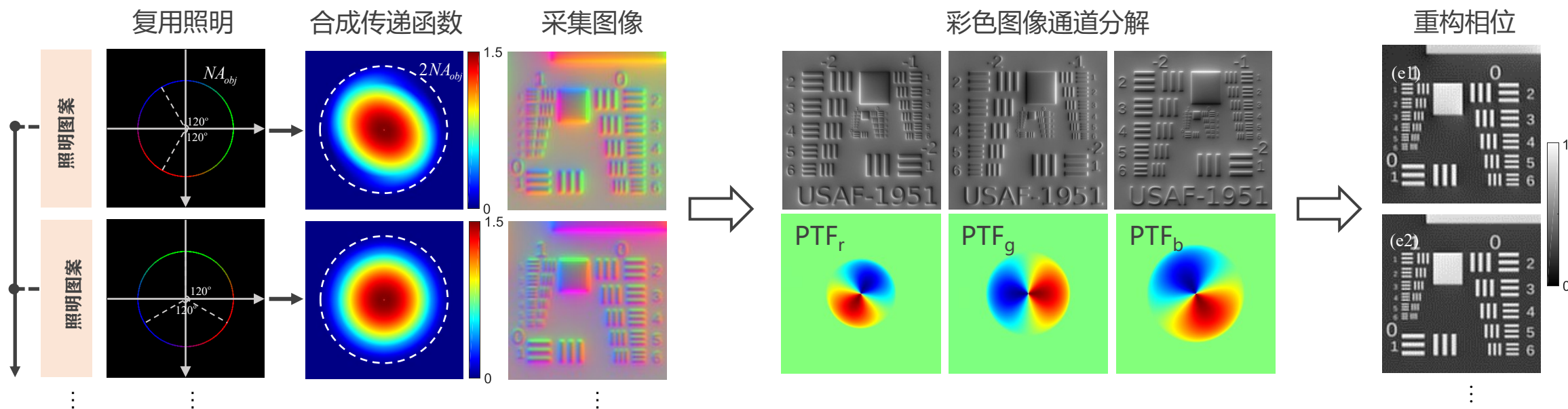
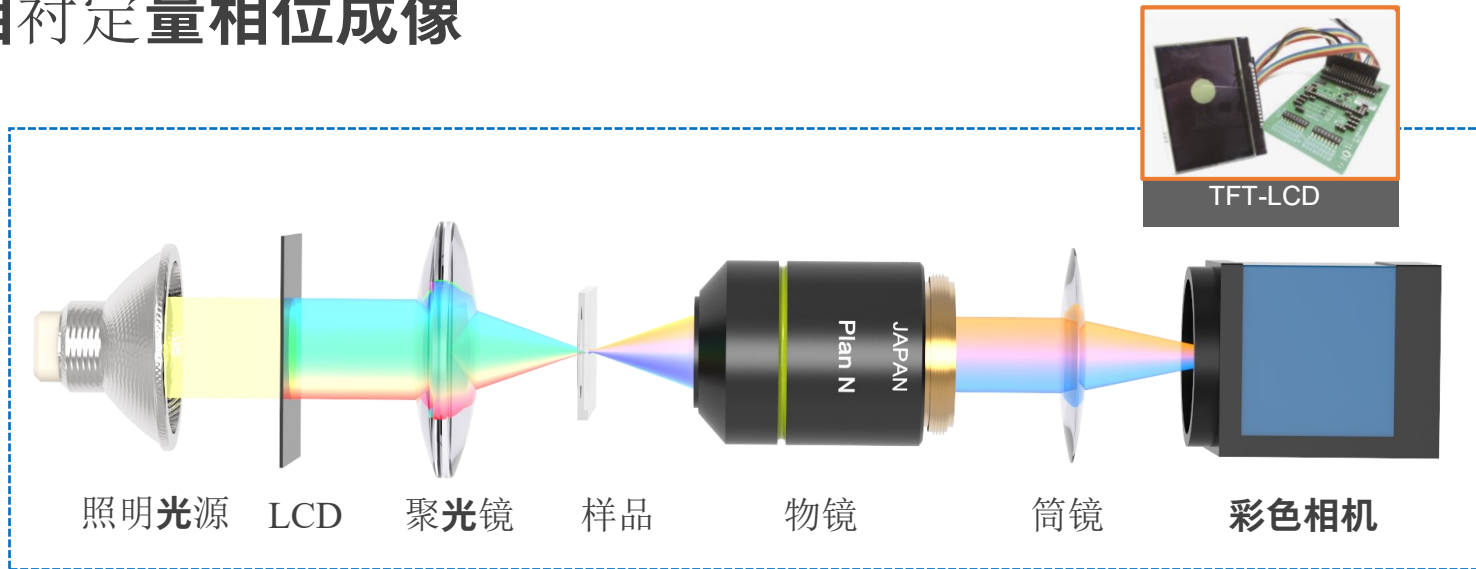
复用照明函数分布

$$S_r(\rho, \theta) = \delta(\rho - NA_{obj}) \sin(\theta + \theta_r)$$

$$S_g(\rho, \theta) = \delta(\rho - NA_{obj}) \sin(\theta + \theta_g)$$

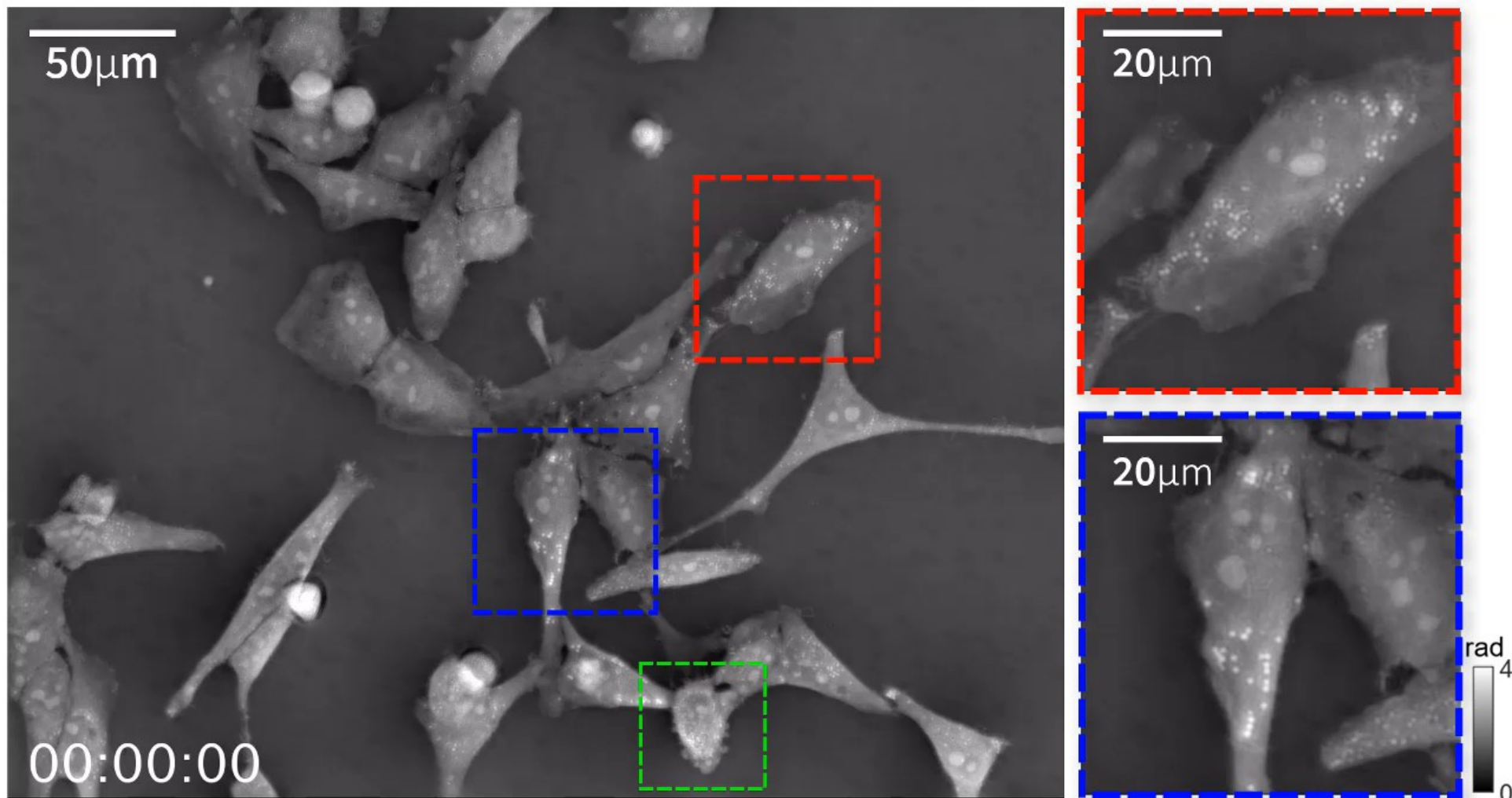
$$S_b(\rho, \theta) = \delta(\rho - NA_{obj}) \sin(\theta + \theta_b)$$

$$(\theta_r = \theta_g - 120^\circ, \theta_b = \theta_g + 120^\circ)$$



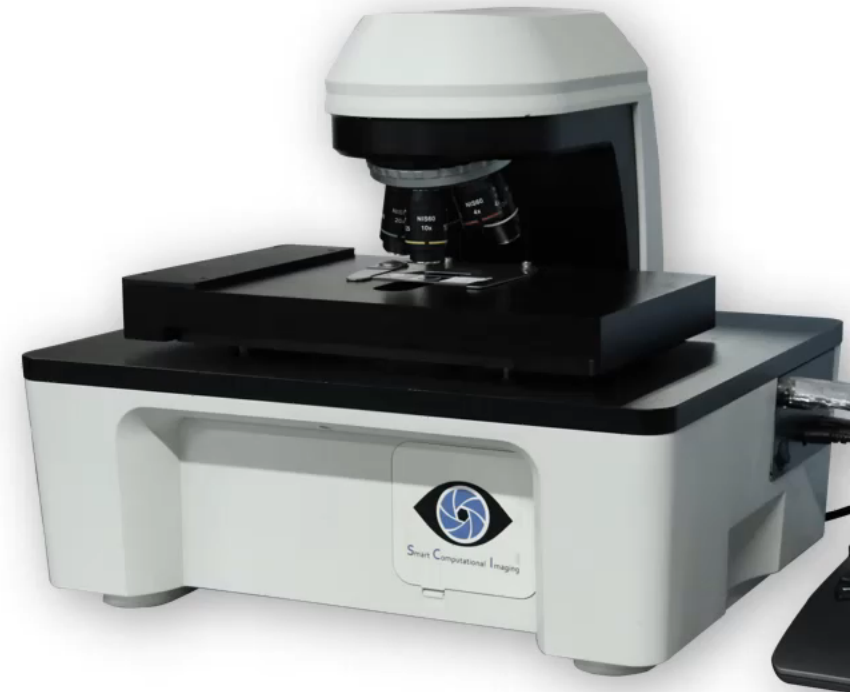
基于彩色复用照明的单帧差分相衬定量相位成像

Hela细胞体外动态定量相位成像(相机帧率30Hz)



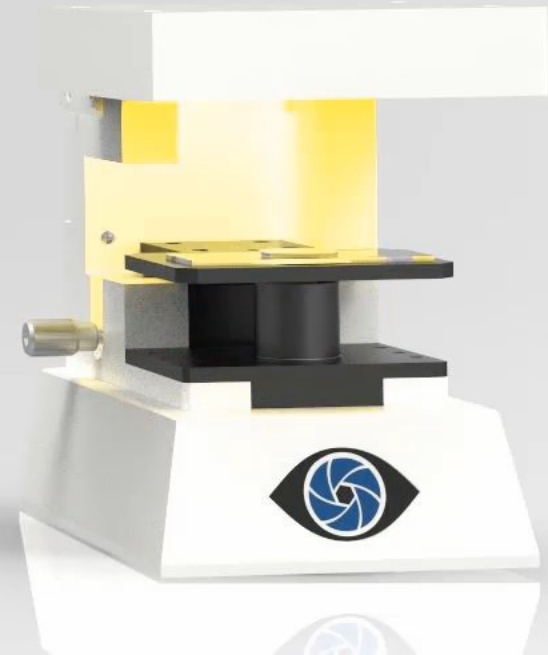
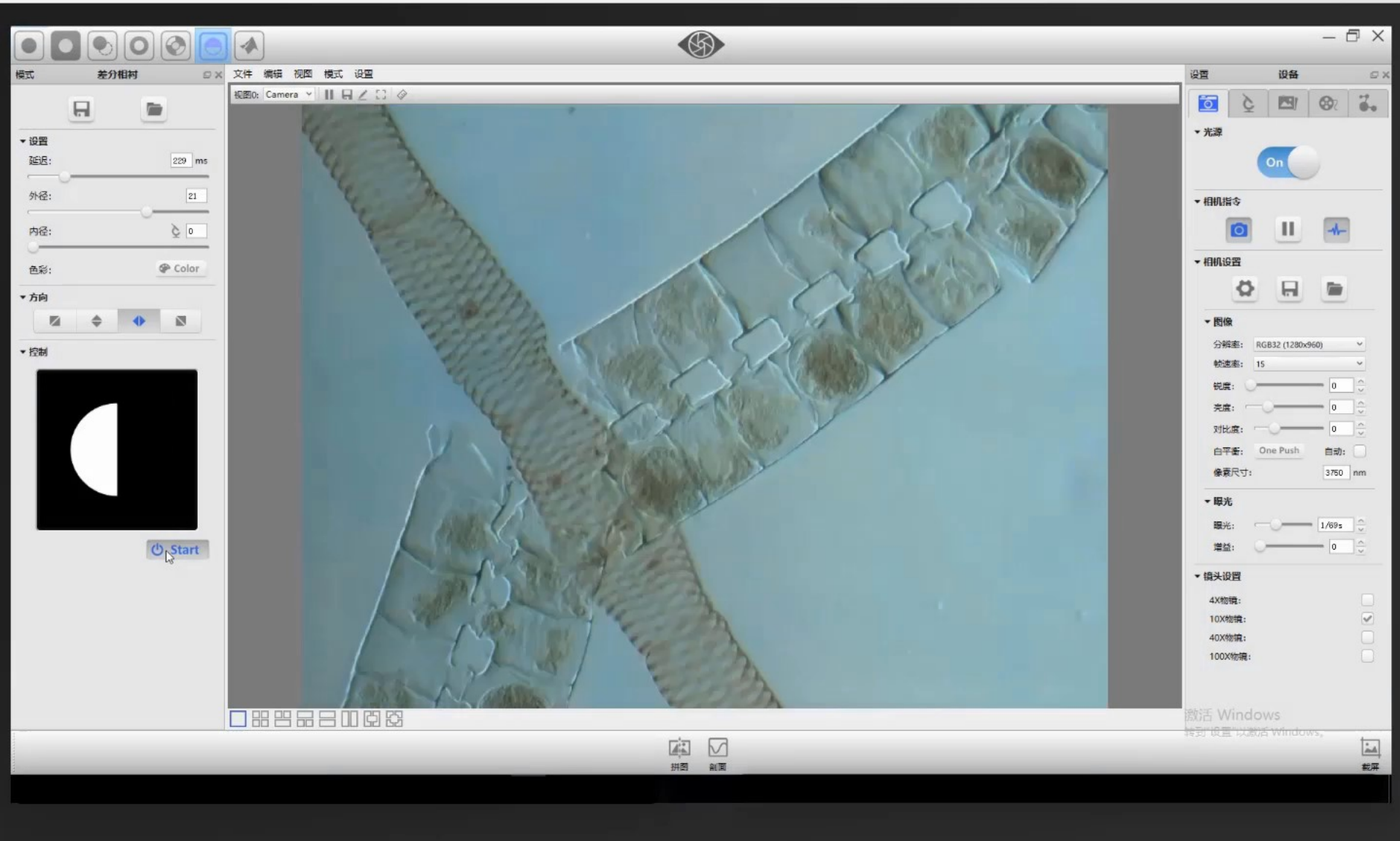
MCQ-CM

Multimode Quantitative Phase Computational Microscopy



MMC-CM frees the user's hands

Flexible control and display



Questions:

定量相位成像方法的分类

定量相位成像方法的优势和劣势